

# **Numerical Prediction of Mesoscale Weather**

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1. History of numerical weather prediction
2. Fundamental equations for atmosphere
3. Importance of the initial condition
4. Ensemble prediction
5. The K-computer project

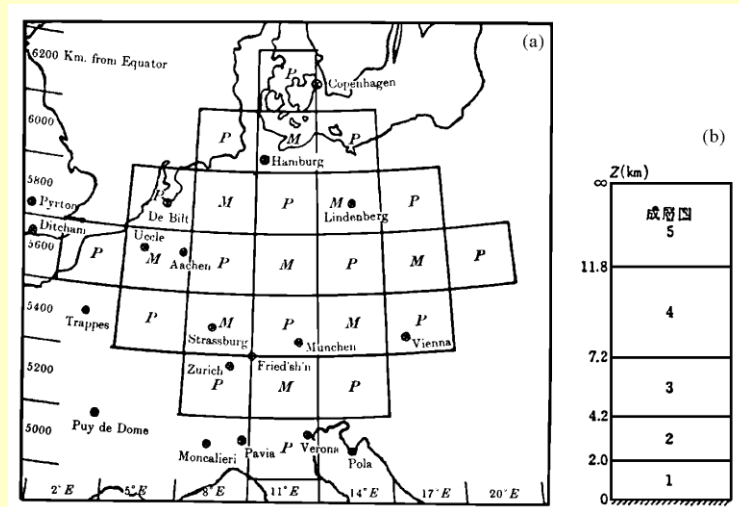
# 1. History of Numerical Weather Prediction

## Numerical Weather Prediction (NWP)

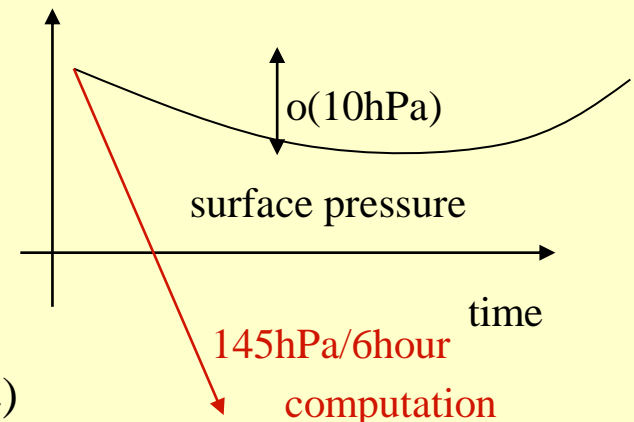
- .. predicts future state of the atmosphere quantitatively by time-integrating laws of physics
- .. regarded as one of the best application fields of computational physics from the earliest period

Bjerknes (1904) pointed out possibility of weather prediction based on dynamics and physics

Richardson (1922) tried weather prediction by solving the equations of fluid with hand calculation but failed by overwhelming of noises



Horizontal and vertical grid taken by Richardson (1922)

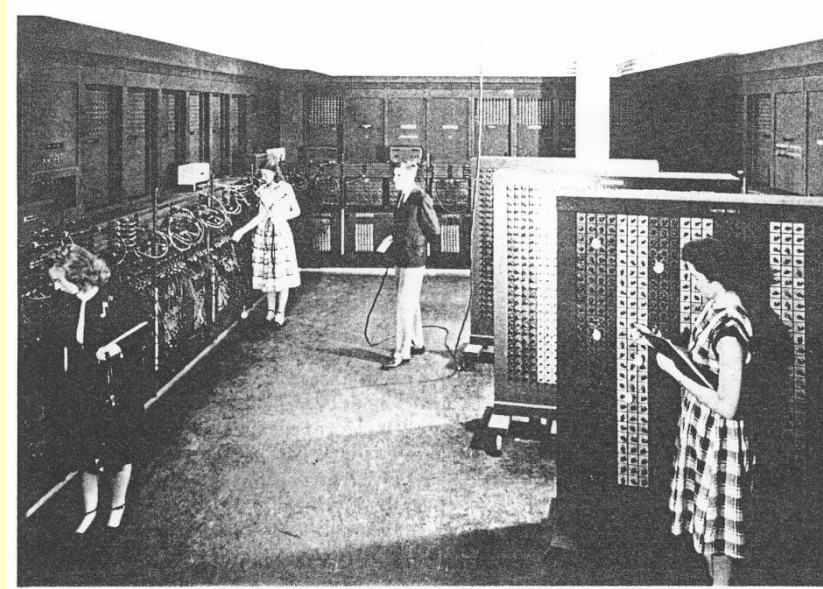


# Dawn of numerical weather prediction

1946 Pennsylvania Univ. Developed the first digital computer (ENIAC)

23 word memories, 18,800 tubes  
(300FLOPS)

Von Neumann of Institute for Advanced Study, Princeton Univ. proposed application to weather prediction



1950 First success of 24 hour forecast using ENIAC by Charney et al.

Grid distance 736 km at 45N

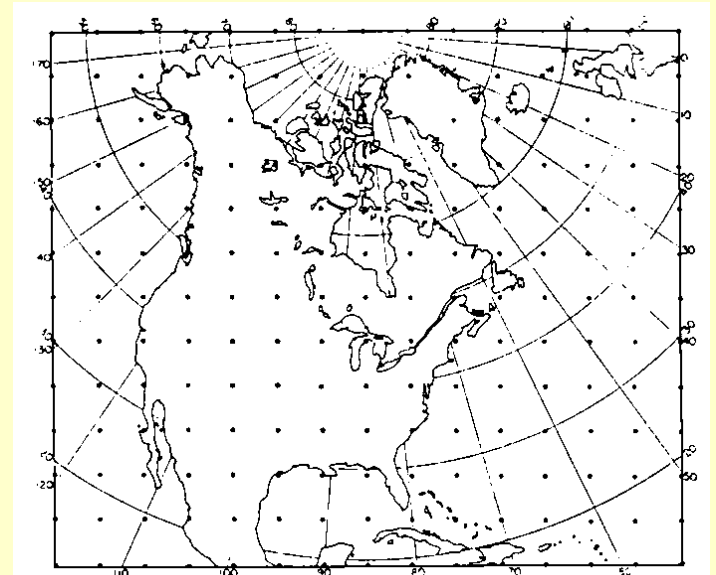
Number of grid points  $15 \times 18$

One level (500hPa)

2-dimensional barotropic model which predicts the absolute vorticity preservation law

$$d/dt(f + \zeta) = 0$$

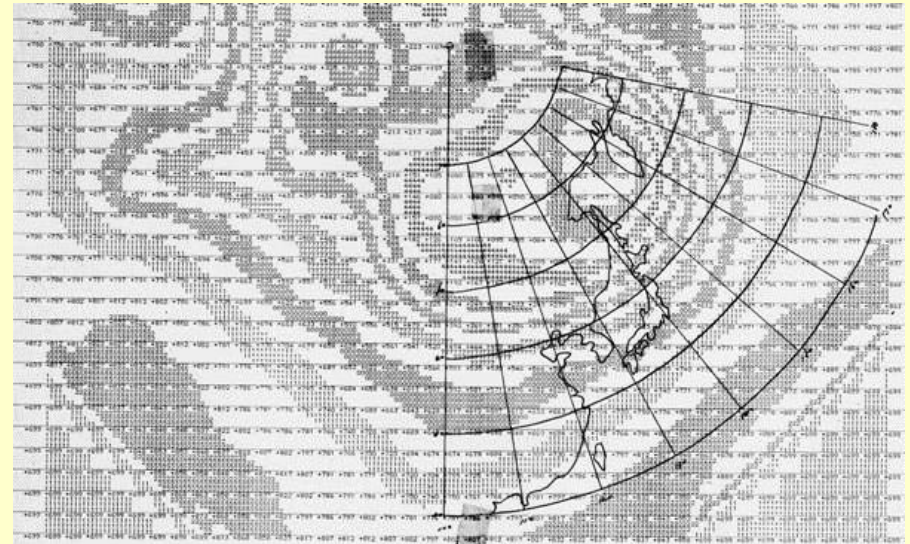
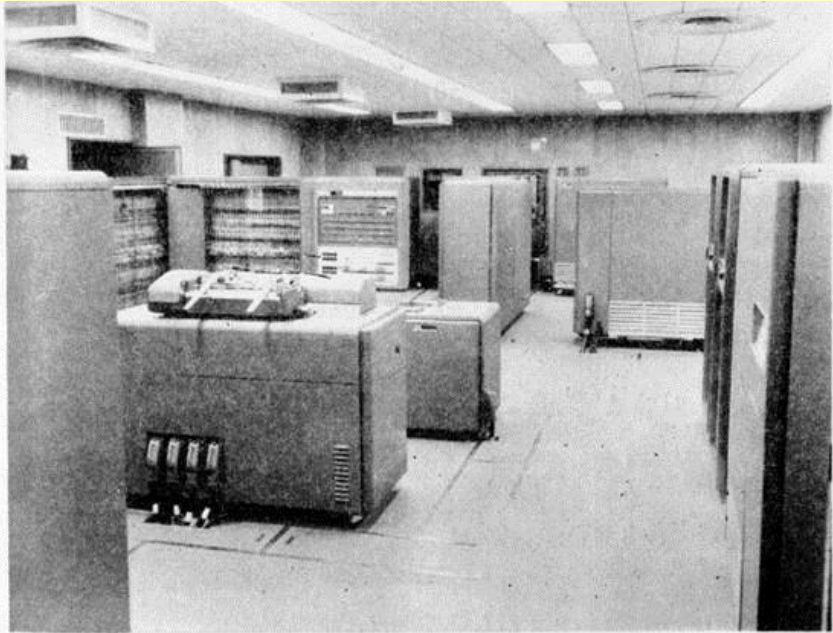
35 days for two 24 hour computations



# NWP in Japan

1959 Japan Meteorological Agency implemented IBM704  
core Memory of 8 K words (36 bit)

1960 Operation started with a northern hemispheric barotropic model  
(381 km, one level)





## 2. Fundamental equations for atmosphere

Six variables which describe the state of dry atmosphere:

three velocity components, pressure, temperature and density

### Prognostic equations

- Momentum equation (three wind components:  $u$ ,  $v$  and  $w$  )
- Continuity equation (pressure:  $p$ )
- Thermodynamic equation (temperature:  $T$ )

### Diagnostic equation

- State equation (density:  $\rho$ )

In the case of moist atmosphere, preservation of water substances and the phase change must be considered (cloud micro-physics).

# Momentum equation

- Momentum equation (three components)

$$\frac{du}{dt} + \frac{1}{\rho} \frac{\partial p}{\partial x} = dif .u$$

$\partial$ : partial derivative symbol

$$\frac{dv}{dt} + \frac{1}{\rho} \frac{\partial p}{\partial y} = dif .v$$

$$\frac{dw}{dt} + \frac{1}{\rho} \frac{\partial p}{\partial z} + g = dif .w$$

▪ Newton's law of motion: (Force) = (mass  $\times$  acceleration)

→

Navier-Sokes' equation for fluid:

(acceleration) = (pressure gradient force per unit mass)

(+diffusion+gravity force for vertical direction )

# Momentum equation

- Momentum equation (three components)

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$\partial$ : partial derivative symbol

▪ Newton's law of motion: (Force) = (mass  $\times$  acceleration)

→

Navier-Sokes' equation for fluid:

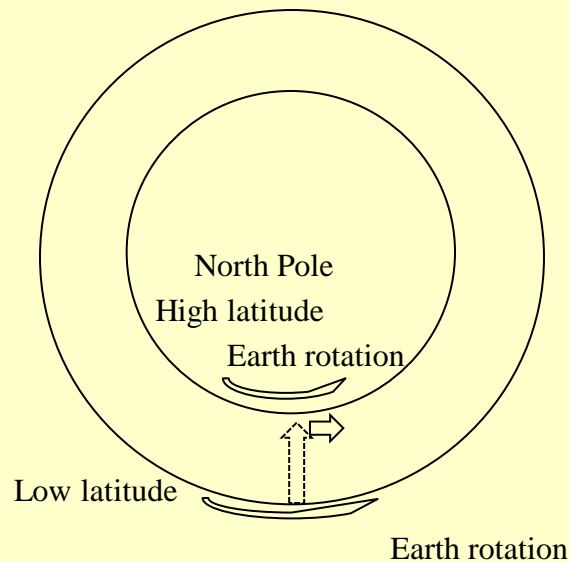
(acceleration) = (pressure gradient force per unit mass)

(+diffusion+gravity acceleration for vertical direction )



# Coriolis' force

Effect of Coriolis' force is added on the earth



Northward motion shifts eastward in Northern hemisphere due to the difference of speeds of earth rotation.

In vector formulation, Coriolis' force is vector product of angular velocity of the earth rotation  $\vec{\Omega}$  and wind vector  $\vec{V}$ :

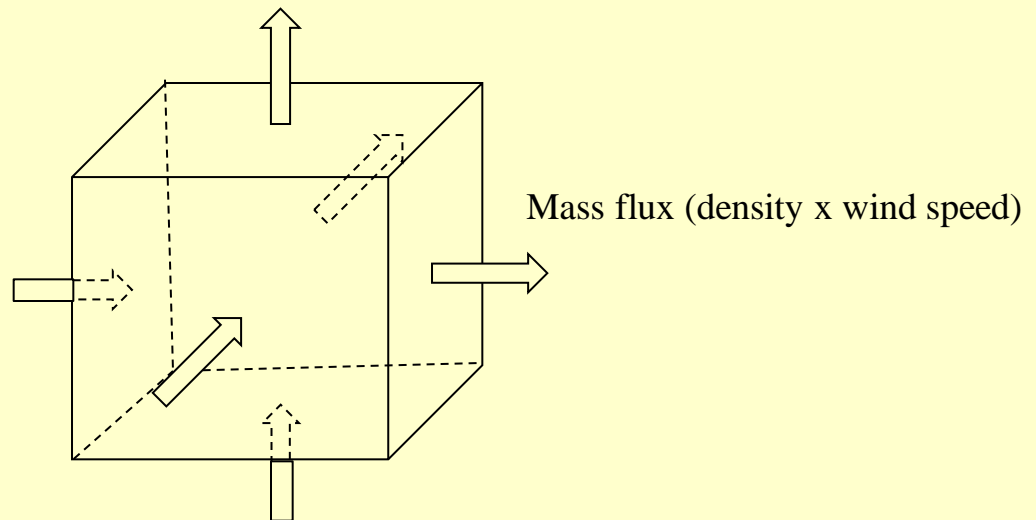
$$\frac{d\vec{V}}{dt} = (-2\vec{\Omega} \times \vec{V}) - \frac{1}{\rho} \nabla p + \vec{g} + \vec{F},$$

# Continuity equation

Continuity equation (law of mass preservation)

$$\frac{\partial \rho}{\partial t} + \frac{\partial \rho u}{\partial x} + \frac{\partial \rho v}{\partial y} + \frac{\partial \rho w}{\partial z} = 0$$

· · local time tendency of density = differences of mass flux through surrounding boundaries



# State equation for ideal gasses

Boyle-Charles's combined law for ideal gas with a molecular weight of  $m$

$$p = \rho \frac{R^*}{m} T = \frac{M}{m} \frac{R^*}{V} T$$

$R^*$  : universal gas constant (=8.314J/mol/K)

In case of dry air (represented by subscript  $d$ ),

by Dalton's law for partial pressure,

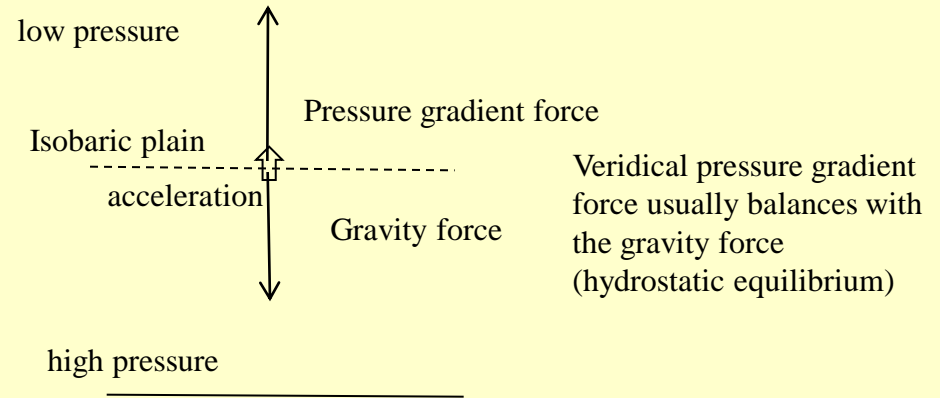
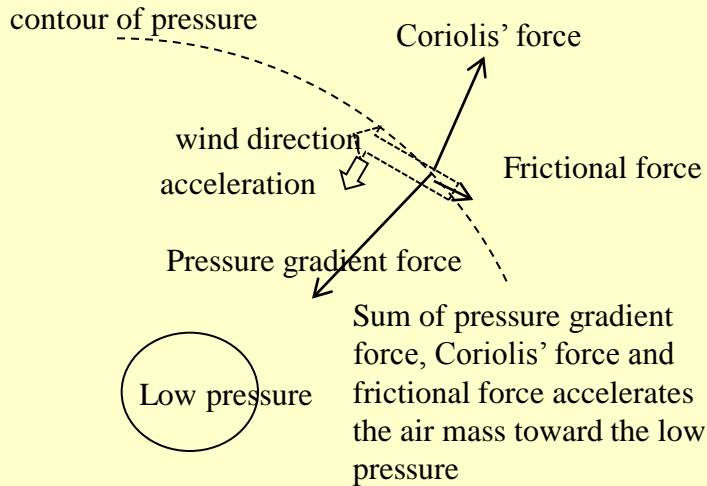
$$p_d = \sum_i p_i = \frac{R^*}{V} T \sum_i \frac{M_i}{m_i} = \frac{R^*}{V} T \frac{\sum_i M_i}{m_d} = \rho_d RT$$

$i$  is index to represent gas component such as nitrogen, oxygen, and argon, and  $m_d$  the weigh-average molecular of dry air (28.966 g/mol)

$$m_d = \frac{\sum_i M_i}{\sum_i \frac{M_i}{m_i}}$$

$R (=R^*/m_d)$  : gas constant for dry air (=287.05 J/Kg/K)

# Forces on air and acceleration



hydrostatic equilibrium  $\frac{1}{\rho} \frac{dp}{dz} + g = 0$

$$\rightarrow \frac{1}{p} \frac{dp}{dz} = -\frac{g}{RT} \quad \rightarrow \frac{d}{dz} (\log p) = -\frac{g}{RT}$$

$$\rightarrow p = p_0 e^{-\frac{gz}{RT_m}}$$

... well-known barometric height formula  
(pressure-height equation)

# Thermodynamic equation

First law of the thermodynamics

$$dQ = dI + pd\alpha$$

· · heating to air mass is the sum of internal energy increase and mechanical work by pressure. Here,  $Q$  is the adiabatic heating rate and  $\alpha$  is specific volume (inverse of density).

$$\begin{aligned} Qdt &= C_v dT + pd\alpha = C_v dT + d(p\alpha) - \alpha dp \\ &= (C_v + R)dT - \alpha dp = C_p dT - \alpha dp \end{aligned}$$

Here  $C_v$  is the specific heat of air at constant volume ( $=5R/2$ ), and  $C_p$  the specific heat of air at constant pressure

# Finite discretization

In the numerical model, differential equation is discretized by finite difference, based on the Taylor series expansion:

$$f(x + \Delta x) = f(x) + \Delta x f'(x) + \frac{(\Delta x)^2}{2} f''(x) + \dots$$

$$f(x - \Delta x) = f(x) - \Delta x f'(x) + \frac{(\Delta x)^2}{2} f''(x) - \dots$$

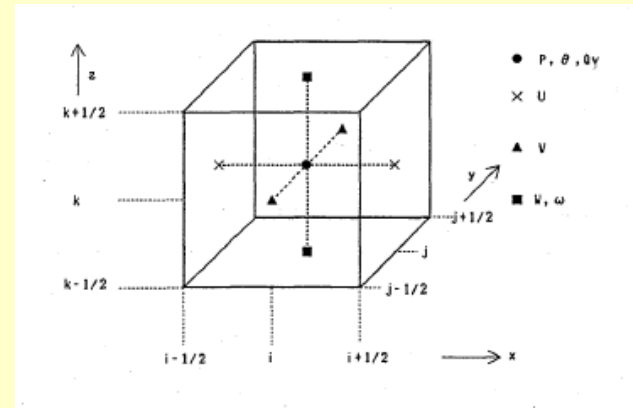
Here,  $f'$  ( $f''$ ) is the first (second) derivative of the function  $f$ .

The second order centered difference can be obtained as :

$$\frac{\partial f}{\partial x} = \frac{f(x + \Delta x) - f(x - \Delta x)}{2\Delta x} + O(\Delta x)^2$$

or, in staggered grid,

$$\frac{\partial f}{\partial x} = \frac{f(x + \frac{\Delta x}{2}) - f(x - \frac{\Delta x}{2})}{\Delta x} + O(\frac{\Delta x}{2})^2$$



For advection term in momentum equations, higher order schemes are used e.g.,

$$\frac{\partial f}{\partial x} = \frac{9}{8} \frac{f(x + \frac{\Delta x}{2}) - f(x - \frac{\Delta x}{2})}{\Delta x} - \frac{1}{8} \frac{f(x + \frac{3\Delta x}{2}) - f(x - \frac{3\Delta x}{2})}{3\Delta x} + O(\frac{\Delta x}{2})^4$$

# Pressure equation and implicit treatment

Pressure equation is obtained from the continuity equation and the state equation:

$$\frac{\partial p}{\partial t} + C_s^2 \left( \frac{\partial \rho u}{\partial x} + \frac{\partial \rho v}{\partial y} + \frac{\partial \rho w}{\partial z} \right) = FP$$

Here,  $C_s$  is the sound wave speed ( $= (C_p/C_v \times RT)^{1/2}$ ) and FP represents forcing term such as the time tendency of (potential) temperature. Solutions of above equations include sound waves due to the elasticity of air. In atmospheric models for weather predication, pressure is treated implicitly in the vertical direction. The following 1-dimensional elliptic (Helmholtz-type) pressure equation is obtained:

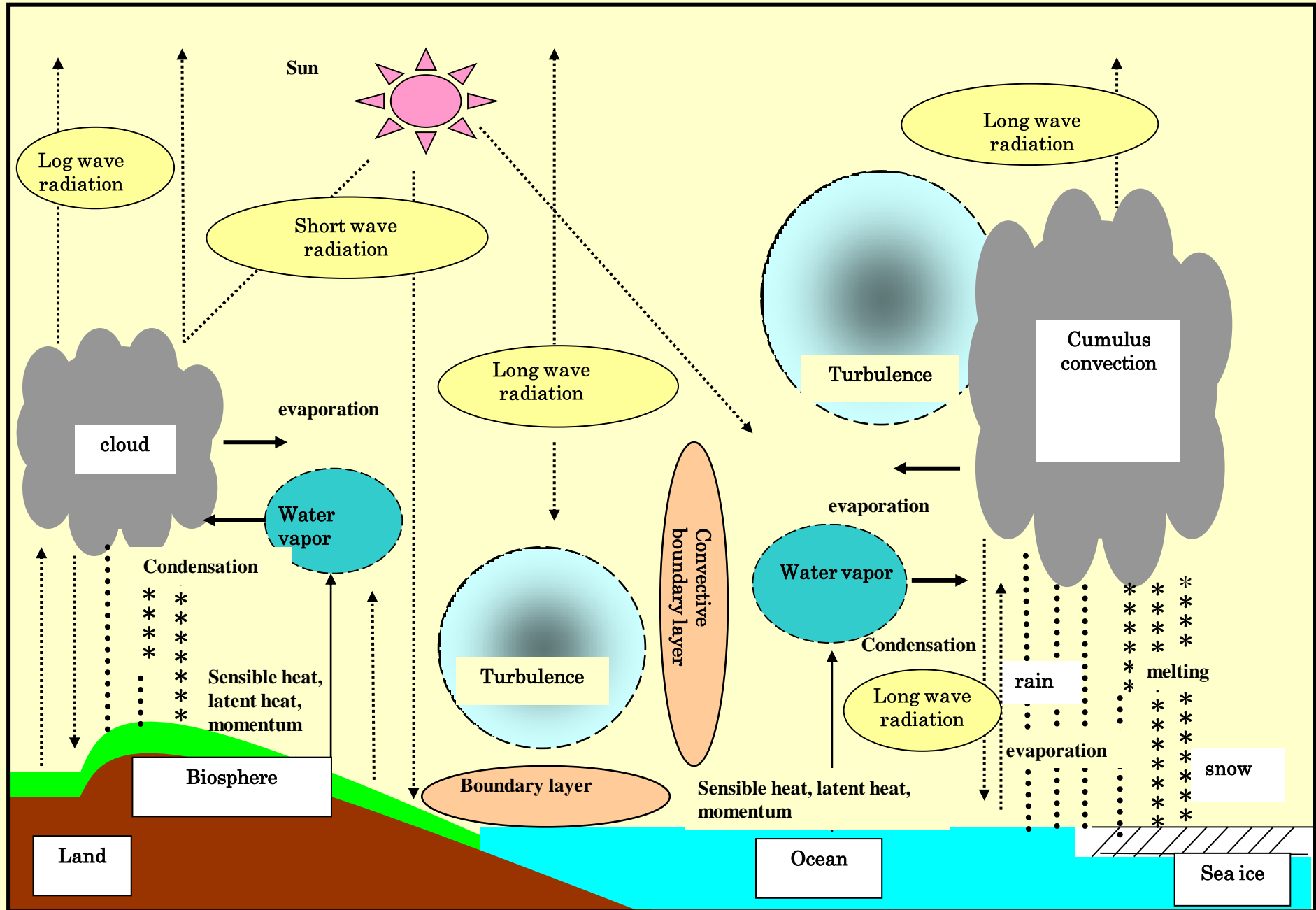
$$\frac{\partial^2 \overline{P^\tau}}{\partial z^2} + \frac{\partial}{\partial z} (\overline{hP^\tau}) + e' \overline{P^\tau} = FP.HE$$

$$\frac{\partial A}{\partial t} = \frac{A^{\tau+\Delta\tau} - A^\tau}{\Delta\tau}, \quad e' = -\left\{ \frac{2}{(1+\beta)\Delta\tau C_s} \right\}^2,$$

$$FP.HE = -\frac{2}{(1+\beta)\Delta\tau} \frac{FP}{C_s^2} + \frac{\partial}{\partial z} FW + \frac{2}{(1+\beta)\Delta\tau} \left\{ \left( \frac{\partial \overline{\rho u^\tau}}{\partial x} + \frac{\partial \overline{\rho v^\tau}}{\partial y} \right) + \frac{\partial \overline{\rho w^\tau}}{\partial z} \right\} + e' \overline{P^\tau}.$$

Gaussian sweep-out elimination method is used to solve above equation.

# Physical processes in NWP model







# Bulk cloud microphysics

In bulk method, the size distribution function of water substance is expressed by the inverse exponential function of the particle diameter  $D$ .

$$N(D) = N_0 e^{-\lambda D}$$

Fall-out terminal velocity of particle is given as a power function of  $D$  by the Stokes' law in the form of

$$V(D) = aD^b$$

Variable $Q_x(\text{kg/kg})$ $N_x(\text{m}^{-3})$	Size distribution $N_x(D) (\text{m}^{-4})$	Fall velocity $U_{dx}(\text{m/s})$	Density $\rho_x(\text{kg/m}^3)$
$Q_r$	$N_r(D) = N_r0 \exp(-\lambda D)$ $N_r0 = 8 \times 10^6$	$a_r D r^{b_r} \left(\frac{\rho_0}{\rho}\right)^{1/2}$ $a_r = 842$ $b_r = 0.8$	$\rho_w = 1 \times 10^3$
$Q_s$ $N_s$	$N_s(D) = N_s0 \exp(-\lambda D)$ $(N_s0 = 1.8 \times 10^6)$	$a_s D s^{b_s} \left(\frac{\rho_0}{\rho}\right)^{1/2}$ $a_s = 17$ $b_s = 0.5$	$\rho_s = 8.4 \times 10$ $r_{s0} = r_0 = 75 \mu\text{m}$ $m_{s0} = (4\pi/3)\rho_s r_{s0}^3$
$Q_g$ $N_g$	$N_g(D) = N_g0 \exp(-\lambda D)$ $(N_g0 = 1.1 \times 10^6)$	$a_g D g^{b_g} \left(\frac{\rho_0}{\rho}\right)^{1/2}$ $a_g = 124$ $b_g = 0.64$	$\rho_g = 3 \times 10^2$ $r_{g0} = r_0 = 75 \mu\text{m}$ $m_{g0} = (4\pi/3)\rho_g r_{g0}^3$
$Q_c$	mono $D_i = \left(\frac{6\rho Q_c}{\pi\rho_w N_c}\right)^{1/3}$ $N_c = 1 \times 10^8 \text{m}^{-3}$	$a_c D c^{b_c}$ $a_c = 3 \times 10^7$ $b_c = 2.0$	$\rho_c = 1.0 \times 10^3$
$Q_i$ $N_i$	mono $D_i = \left(\frac{6\rho Q_i}{\pi\rho_i N_i}\right)^{1/3}$	$a_i D i^{b_i} \left(\frac{\rho_0}{\rho}\right)^{0.35}$ $a_i = 7 \times 10^2$ $b_i = 1.0$	$\rho_i = 1.5 \times 10^2$ $m_{i0} = 1 \times 10^{-12} \text{kg}$

# Bulk cloud microphysics

The mass-weighted mean velocity is obtained by

$$\bar{V} = \frac{\int \frac{\pi}{6} \rho_w D^3 V(D) N(D) dD}{\int \frac{\pi}{6} \rho_w D^3 N(D) dD} = \frac{\int D^3 a D^b e^{-\lambda D} dD}{\int D^3 e^{-\lambda D} dD} = \frac{a \Gamma(4+b)}{6 \lambda^b}$$

Here  $\Gamma(x)$  is the Gamma function

$$\Gamma(z) = \int_0^{\infty} t^{z-1} e^{-t} dt$$

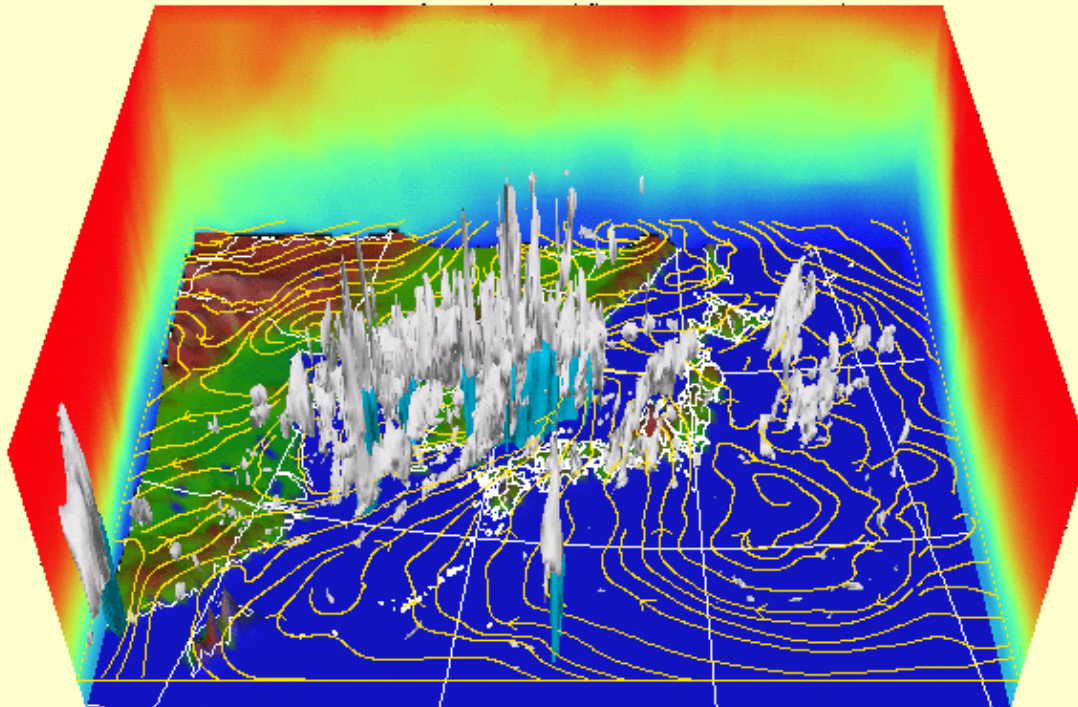
By Euler's partial integration, the Gamma function has the following characteristic

$$\begin{aligned} \Gamma(z) &= \int_0^{\infty} t^{z-1} (-e^{-t})' dt = \left[ -t^{z-1} e^{-t} \right]_0^{\infty} + (z-1) \int_0^{\infty} t^{z-2} e^{-t} dt \\ &= (z-1) \Gamma(z-1) \end{aligned}$$

# JMA nonhydrostatic model (Sep. 2004)

Mesoscale model of JMA which does not use approximation of the hydrostatic equilibrium

- *Fully compressible numerics developed by MRI and NPD*
- *3 ice bulk cloud microphysics with the Kain-Fritsch convective parameterization scheme*
- *Non-local boundary layer scheme*



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## The Operational JMA Nonhydrostatic Mesoscale Model

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### ABSTRACT

An operational nonhydrostatic mesoscale model has been developed by the Numerical Prediction Division (NPD) of the Japan Meteorological Agency (JMA) in partnership with the Meteorological Research Institute (MRI). The model is based on the MRI/NPD unified nonhydrostatic model (MRI/NPD-NHM), while several modifications have been made for operational numerical weather prediction with a horizontal resolution of 10 km. A fourth-order advection scheme considering staggered grid configuration is implemented. The buoyancy term is directly evaluated from density perturbations. A time-splitting scheme for advection has been developed, where the low-order (second order) part of advection is modified in the latter half of the leapfrog time integration. Physical processes have also been revised, especially in the convective parameterization and PBL schemes. A turbulent kinetic energy (TKE) diagnostic scheme has been developed to overcome problems that arise to predict TKE. The model performance for mesoscale NWP has been verified by comparison with a former operational hydrostatic mesoscale model of JMA. It is found that the new nonhydrostatic mesoscale model outperforms the hydrostatic model in the prediction of synoptic fields and quantitative precipitation forecasts.

### 1. Introduction

Rapid progress of the computer facilities in recent years enables us to use higher-resolution models in numerical weather prediction (NWP). The horizontal resolution of operational regional/mesoscale models in world main forecast centers is becoming higher and higher and is about 10 km, the limit of validity of the hydrostatic approximation. The Deutscher Wetterdienst (DWD) developed a regional nonhydrostatic

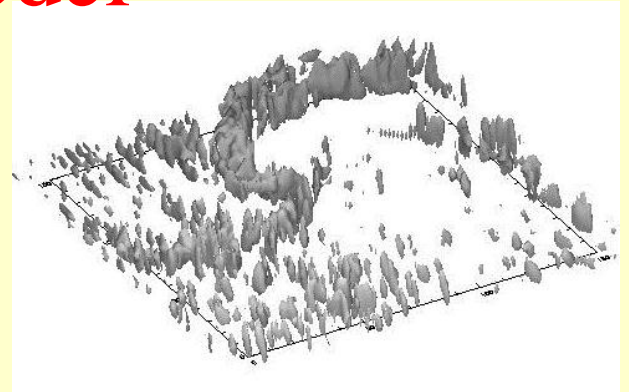
model (the Lokal-Model; Doms and Schättler 1997) and started its operational run with a horizontal resolution of 7 km in 1999. The Met Office introduced nonhydrostatic new dynamics (Davies et al. 2005) in the Unified Model in 2002. The Meteorological Service of Canada, the National Centers for Environmental Prediction of the United States, and other national forecast centers have also been developing or testing their nonhydrostatic NWP models for operation.

In Japan, the Japan Meteorological Agency (JMA) started operational run of a 10-km-resolution mesoscale model in March 2001, and 15-h time integration has been carried out 4 times a day. This model, MSM, was introduced to support information for disaster prevention and is also used for the very short range fore-

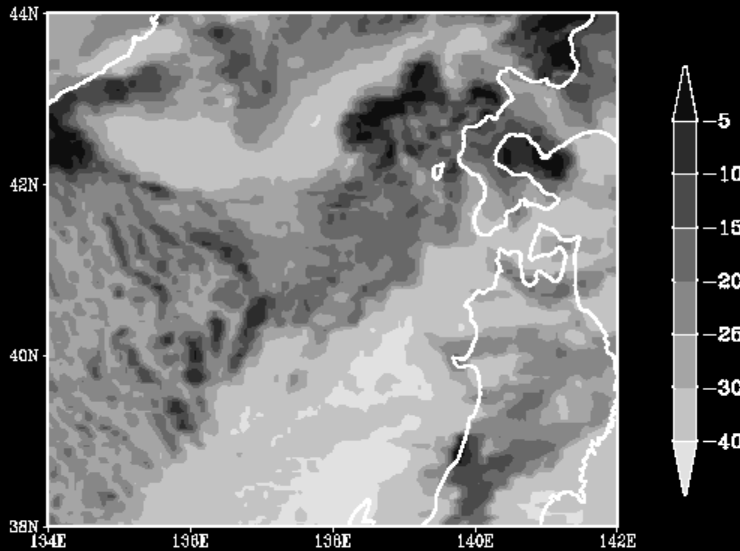
Corresponding author address: Dr. Kazuo Saito, Second Laboratory, Forecast Research Department, Meteorological Research Institute, 1-1 Nagamine, Tsukuba, Ibaraki 305-0852, Japan.  
E-mail: ksaio@met-jma.go.jp

# Cloud resolving model

Polar low simulation with JMA NHM  
Horizontal resolution 2km  
Initial time 15UTC 21 January 1997

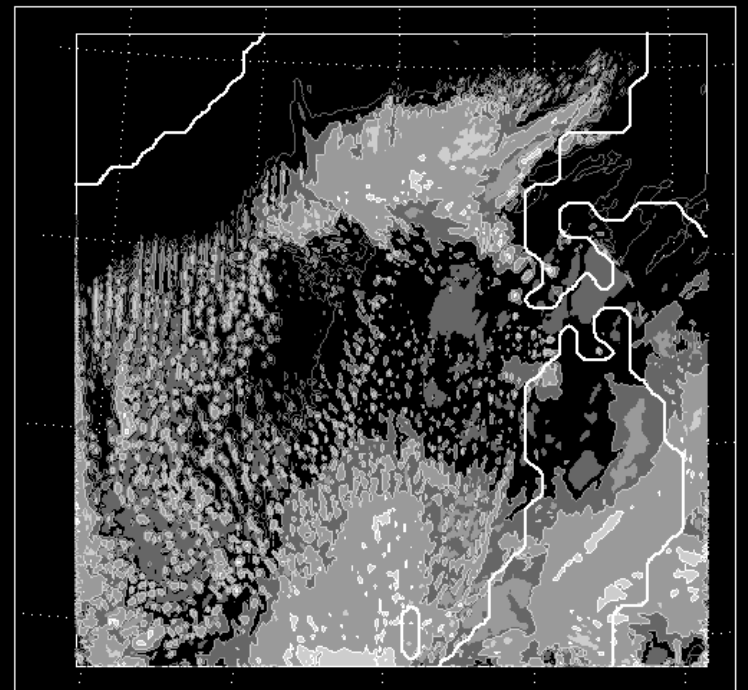


GMS-5 IR Data 1997 JAN 2108UTC



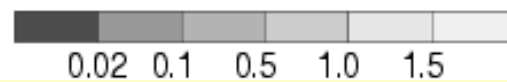
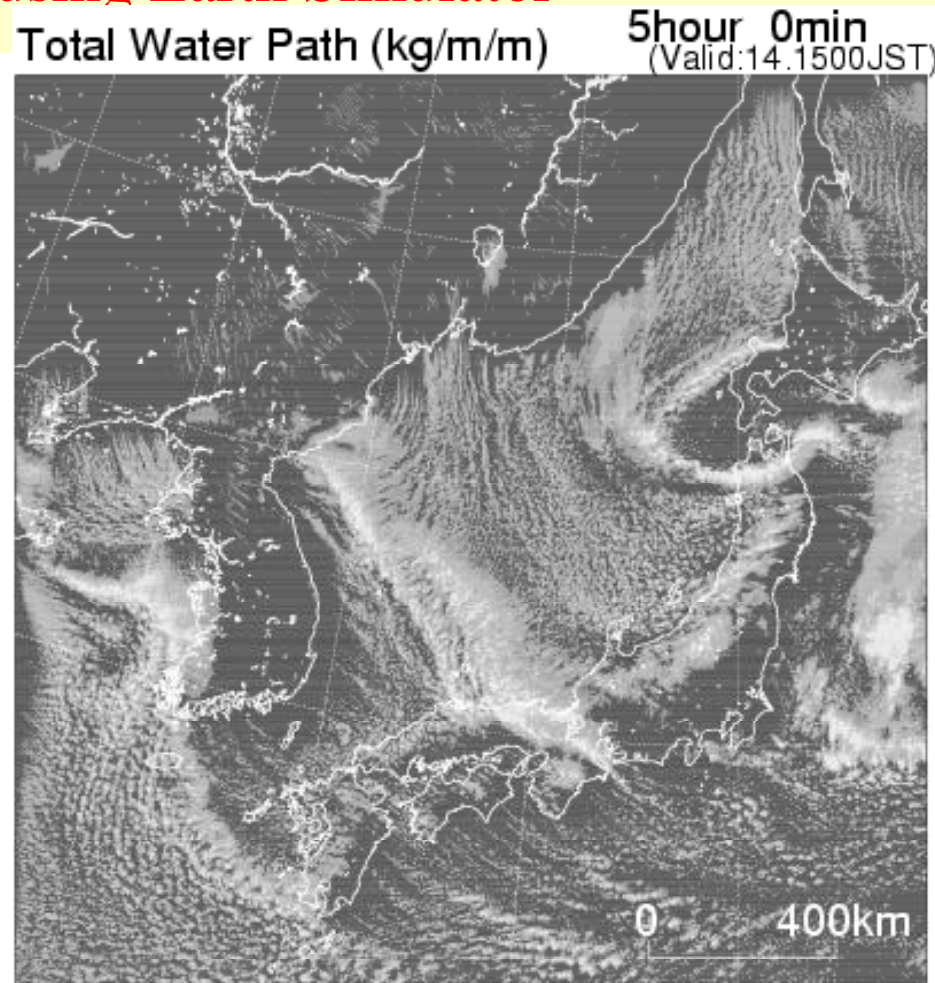
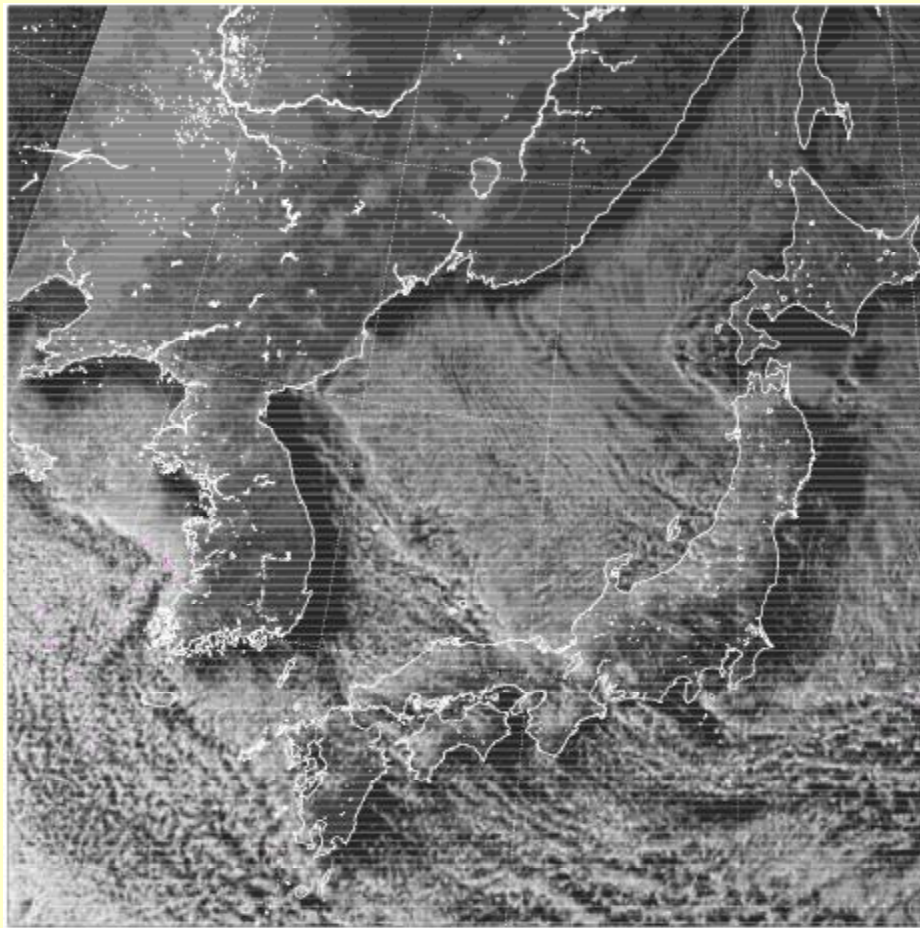
GMS satellite IR image

Accumulated total water 1997 JAN 210750 UTC



Cloud resolving simulation of a polar low (Yanase et al., 2002; GRL)

# Cloud resolving simulation of winter monsoon clouds over the Sea of Japan using Earth Simulator



Left) GMS satellite visible-Image at 15JST 14 January 2001

Right) Total water simulated by NHM with a horizontal resolution of 1 km

Eito et al. (2010; JMSJ)

# 3. Importance of the initial condition

## Major difference between climate projection and NWP

- **the same point**

predict future state of the atmosphere quantitatively by time-integrating laws of physics.

- **major difference**

  - Climate projection**

    - · projects climate response to change of global environment such as CO<sub>2</sub>, SST

    - ⇒ boundary condition and radiation-convection equilibrium are important

  - NWP**

    - · predicts weather of a specific day in short time range

    - ⇒ initial condition and time evolution are important

# Maximum likelihood estimation in data assimilation

- $x$  : analysis variable
- $x_b$  : first guess of  $x$
- $y_o$  : observation data
- $p(\cdot | \cdot)$  : conditional probabilistic density function (PDF)

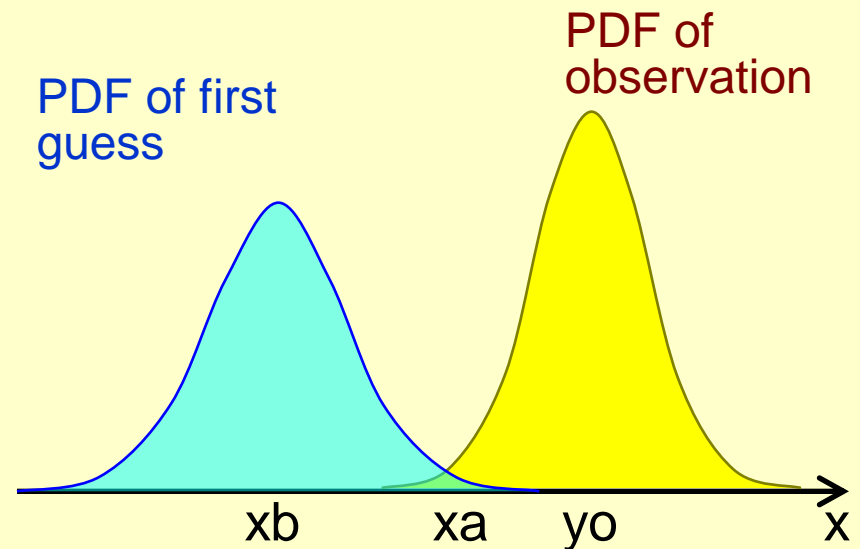
## Bayesian theorem

(if  $x_b$  and  $y_o$  are independent,

$$p(\mathbf{x} | \mathbf{x}_b, \mathbf{y}_o) = \frac{p_b(\mathbf{x}_b)p_o(\mathbf{y}_o)}{\int p_b(\mathbf{x}_b)p_o(\mathbf{y}_o)d\mathbf{x}}$$

## Bayesian estimation

$$\hat{\mathbf{x}} = \max_x [p_b(\mathbf{x}_b)p_o(\mathbf{y}_o)]$$





If PDFs of the first guess and observation are Gaussian normal distribution as

$$p_b(\mathbf{x}_b) = \frac{1}{\sqrt{2\pi\sigma_b^2}} \exp\left\{-\frac{(x-x_b)^2}{2\sigma_b^2}\right\}$$

$$p_o(y_o) = \frac{1}{\sqrt{2\pi\sigma_o^2}} \exp\left\{-\frac{(y-y_o)^2}{2\sigma_o^2}\right\}$$

The conditional PDF of  $x$  with background  $x_b$  and observation  $y_o$  is normal as

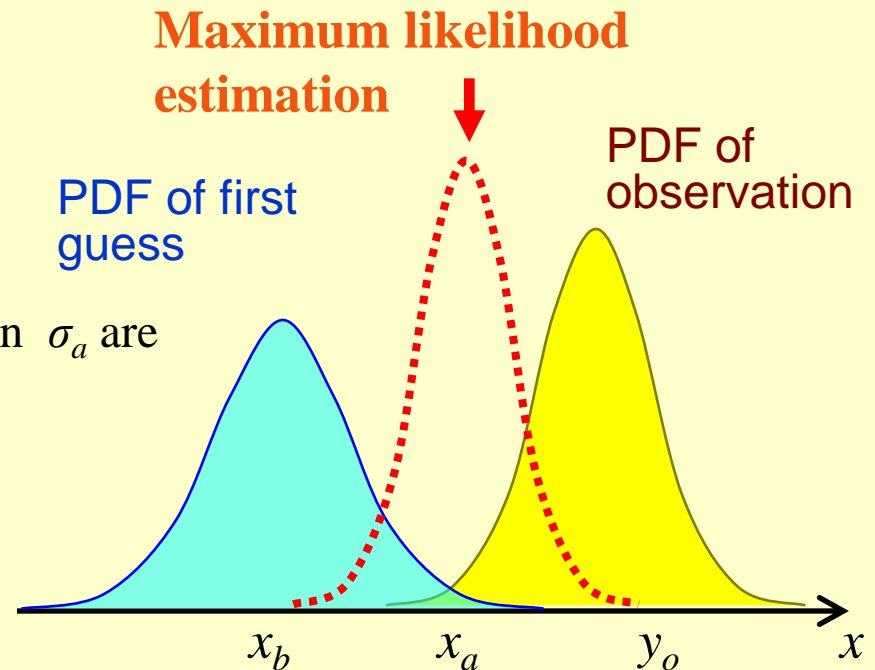
$$p(\mathbf{x} | \mathbf{x}_b, \mathbf{y}_o) = \frac{p_b(\mathbf{x}_b)p_o(\mathbf{y}_o)}{\int p_b(\mathbf{x}_b)p_o(\mathbf{y}_o)d\mathbf{x}}$$

$$= \frac{1}{\sqrt{2\pi\sigma_a^2}} \exp\left\{-\frac{(x-x_a)^2}{2\sigma_a^2}\right\}$$

Where analysis  $x_a$  and its standard deviation  $\sigma_a$  are

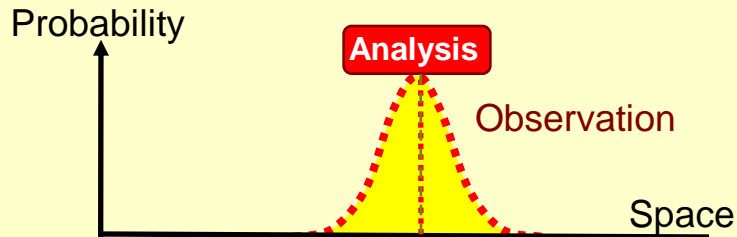
$$\frac{x_a}{\sigma_a^2} = \frac{x_b}{\sigma_b^2} + \frac{y_o}{\sigma_o^2}$$

$$\frac{1}{\sigma_a^2} = \frac{1}{\sigma_b^2} + \frac{1}{\sigma_o^2} \quad \rightarrow \quad x_a = \frac{\sigma_o^2 x_b + \sigma_b^2 y_o}{(\sigma_b^2 + \sigma_o^2)}$$



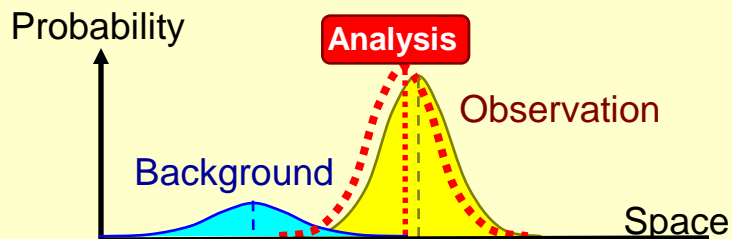
Analysis is weighted mean of first guess and observation, and analysis error becomes smaller than the errors of first guess and observation.

# Relation between 1st guess, observation and analysis



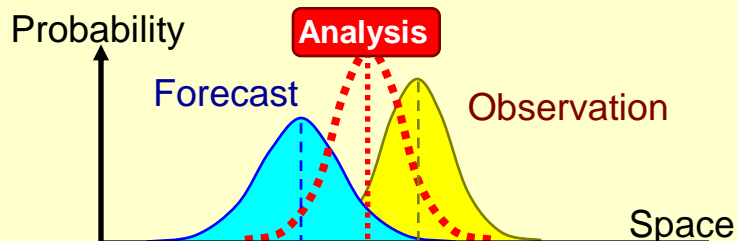
## Simple fitting

- Use observation data only



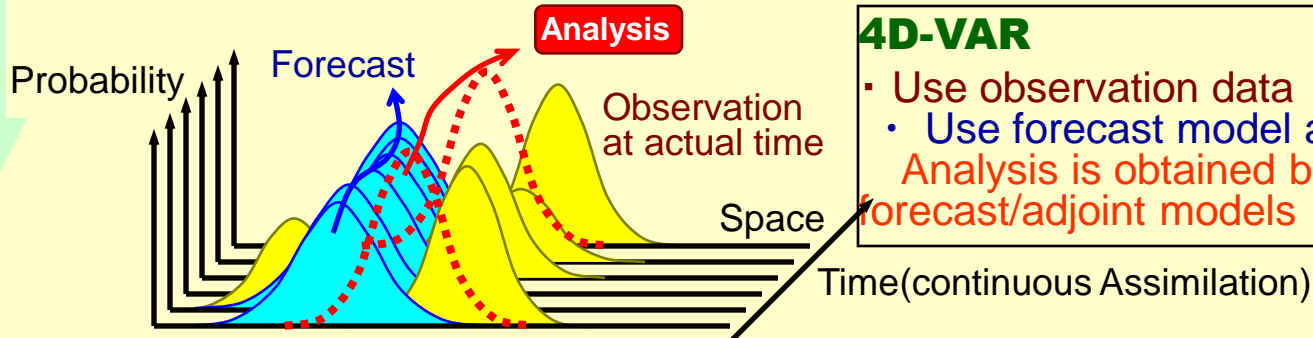
## Correction method

- Use observation data
- Use low quality background information



## Optimal interpolation / 3D-VAR

- Use observation data
- Use forecast as the 1st guess  
background error is given by statistics



## 4D-VAR

- Use observation data
- Use forecast model and 1st guess  
Analysis is obtained by time evolution of forecast/adjoint models

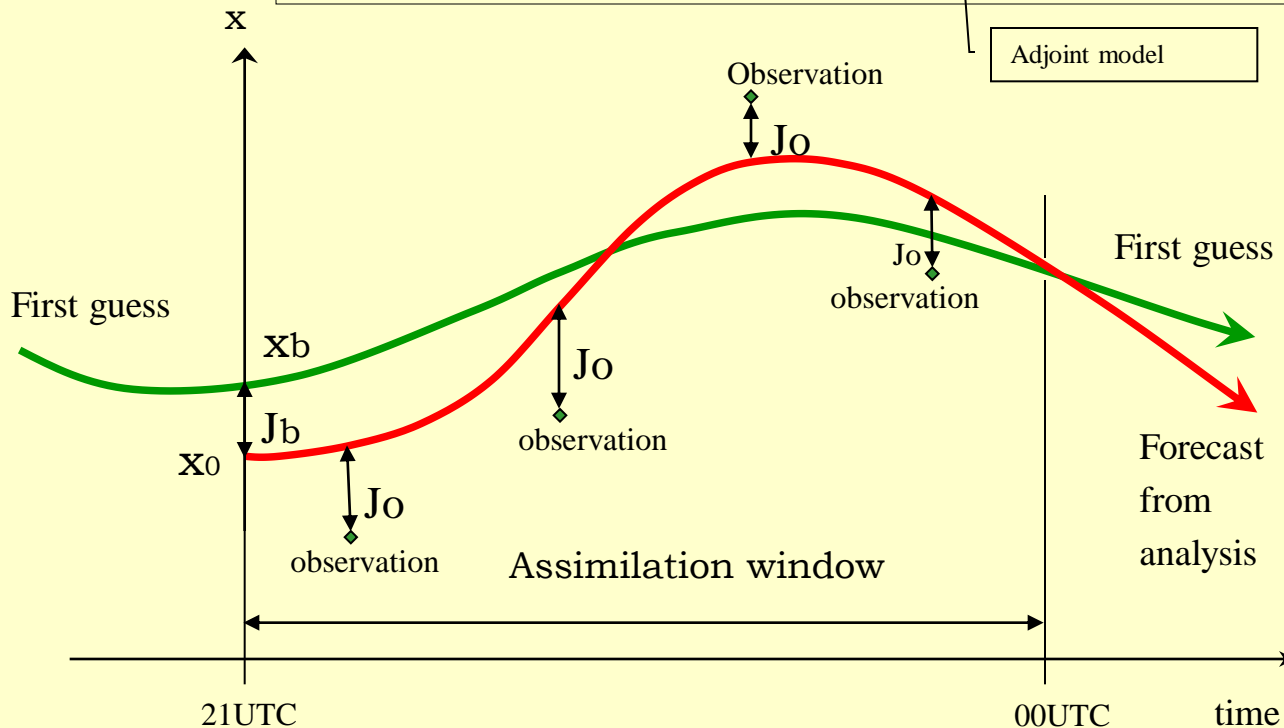
# 4Dimensional – Variational method

**Cost function :**  $J = J_b + J_o + J_c$

$$= \frac{1}{2}(x_0 - x_0^b)^T B^{-1}(x_0 - x_0^b) + \frac{1}{2}(HMx_0 - y^o)^T R^{-1}(HMx_0 - y^o) + J_c$$

**Gradient of cost function:**  $\nabla_{x_0} J = \nabla_{x_0} J_b + \nabla_{x_0} J_o + \nabla_{x_0} J_c$

$$= B^{-1}(x_0 - x_0^b) + M^T H^T R^{-1}(HMx_0 - y^o) + \nabla_{x_0} J_c$$



Observation data can be assimilated at observation time

# 4Dimensional – Variational method

**Cost**

**function :**

$$J = J_b + J_o + J_c$$

Distant from the first guess

$$= \frac{1}{2} (x_0 - x_0^b)^T B^{-1} (x_0 - x_0^b) + \frac{1}{2} (HMx_0 - y^o)^T R^{-1} (HMx_0 - y^o) + J_c$$

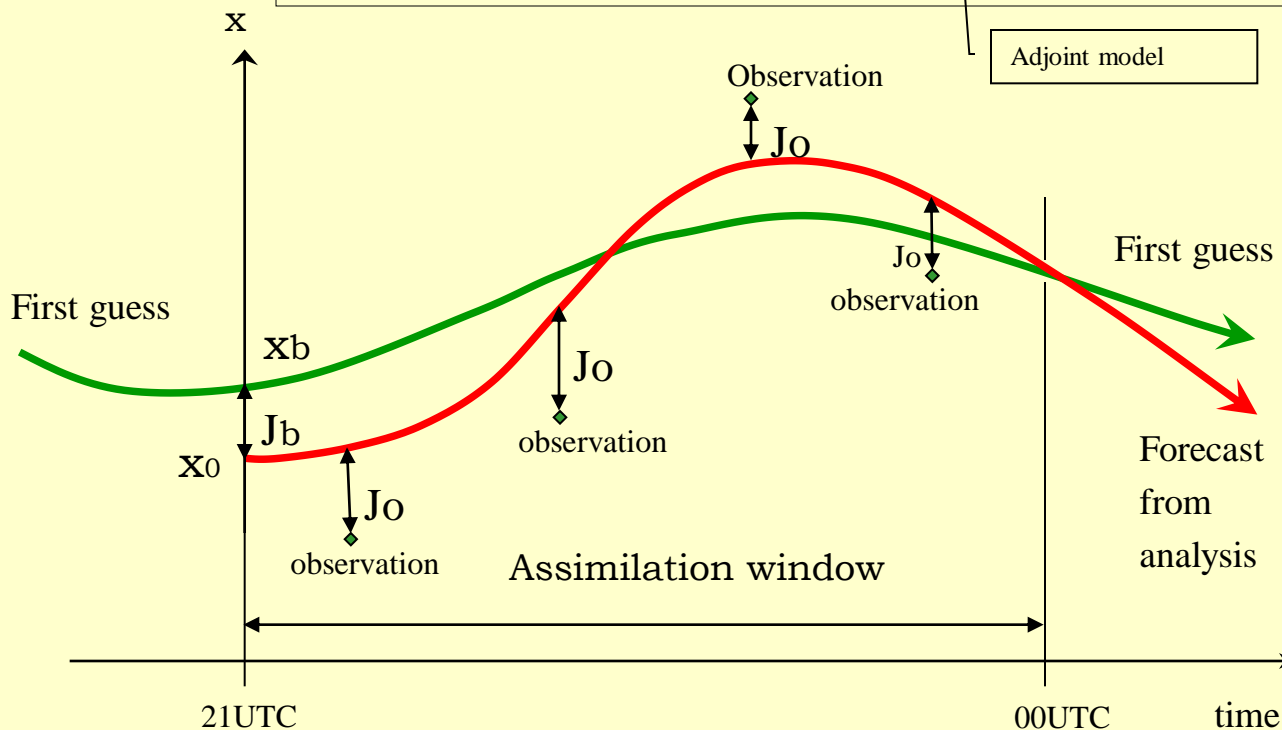
**Gradient of cost function:**

$$\nabla_{x_0} J = \nabla_{x_0} J_b + \nabla_{x_0} J_o + \nabla_{x_0} J_c$$

Distant from observations

**function:**

$$= B^{-1} (x_0 - x_0^b) + M^T H^T R^{-1} (HMx_0 - y^o) + \nabla_{x_0} J_c$$



Observation data can be assimilated at observation time

# Meso 4DVAR (Mar. 2002)

(Koizumi et al., 2005; SOLA)

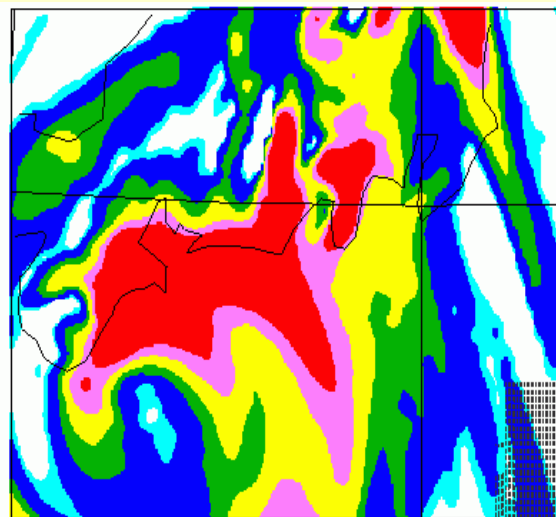
The world first implementation of regional 4DVAR for operation.

LT and ADJ models based on MSM (a hydrostatic spectral model) of JMA.

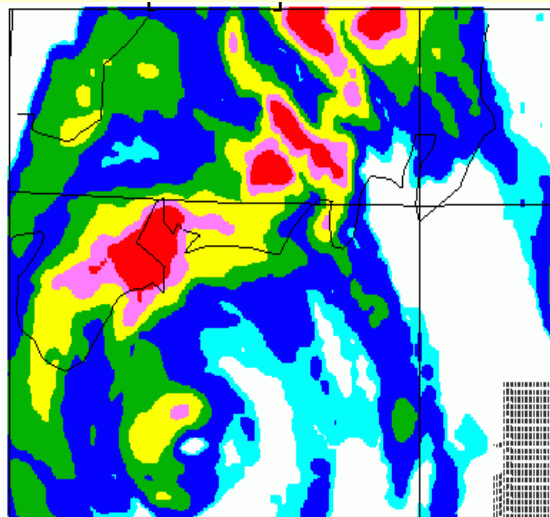
**RUC with PI**

**4D-Var**

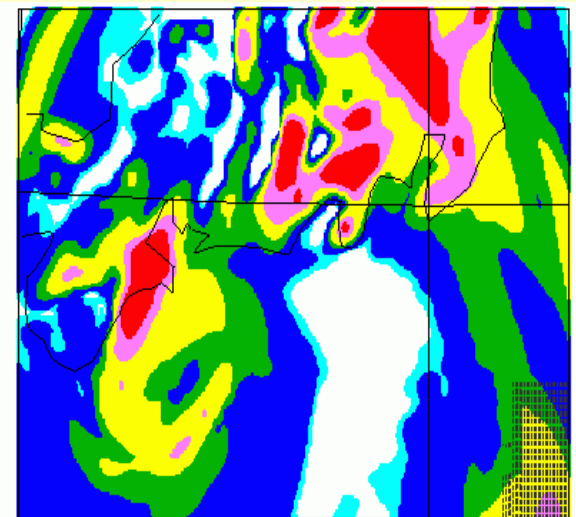
**Observation**



valid: 9/10 03Z - 9/10 06Z



valid: 9/10 03Z - 9/10 06Z



valid: 9/10 03Z - 9/10 06Z

0.5 1.0 5.0 10. 20. 30.

**FT=15-18**

3 hour accumulated rain for FT=18  
Initial 12 UTC 9 September 2001

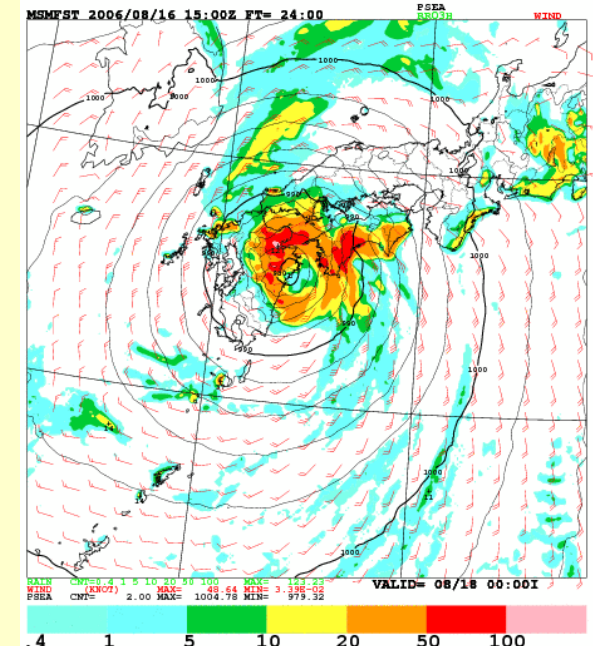
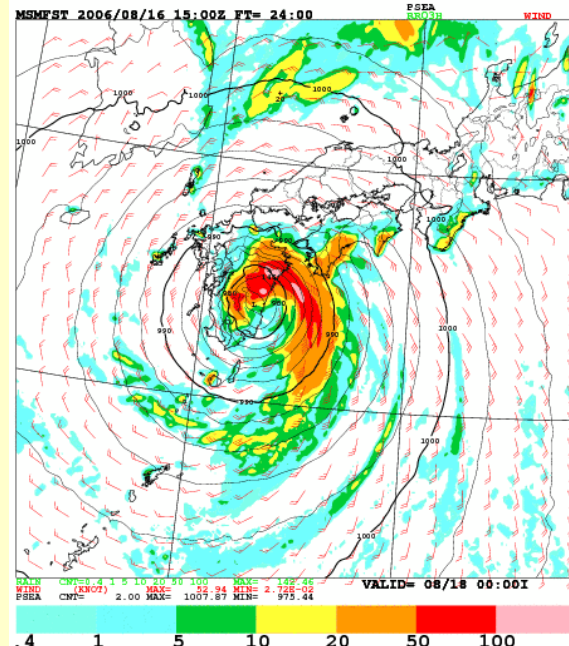
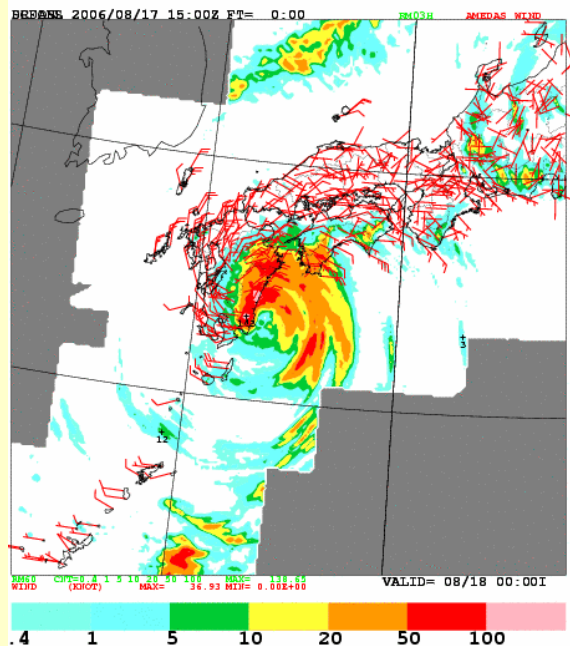
# Nonhydrostatic 4DVAR (Apr. 2009-)

(JNoVA; Honda et al., 2009)

LT and ADJ models based on JMA-NHM

Radar-AMeDAS observation JNoVA (nonhydrostatic)

Meso 4DVAR (hydrostatic)

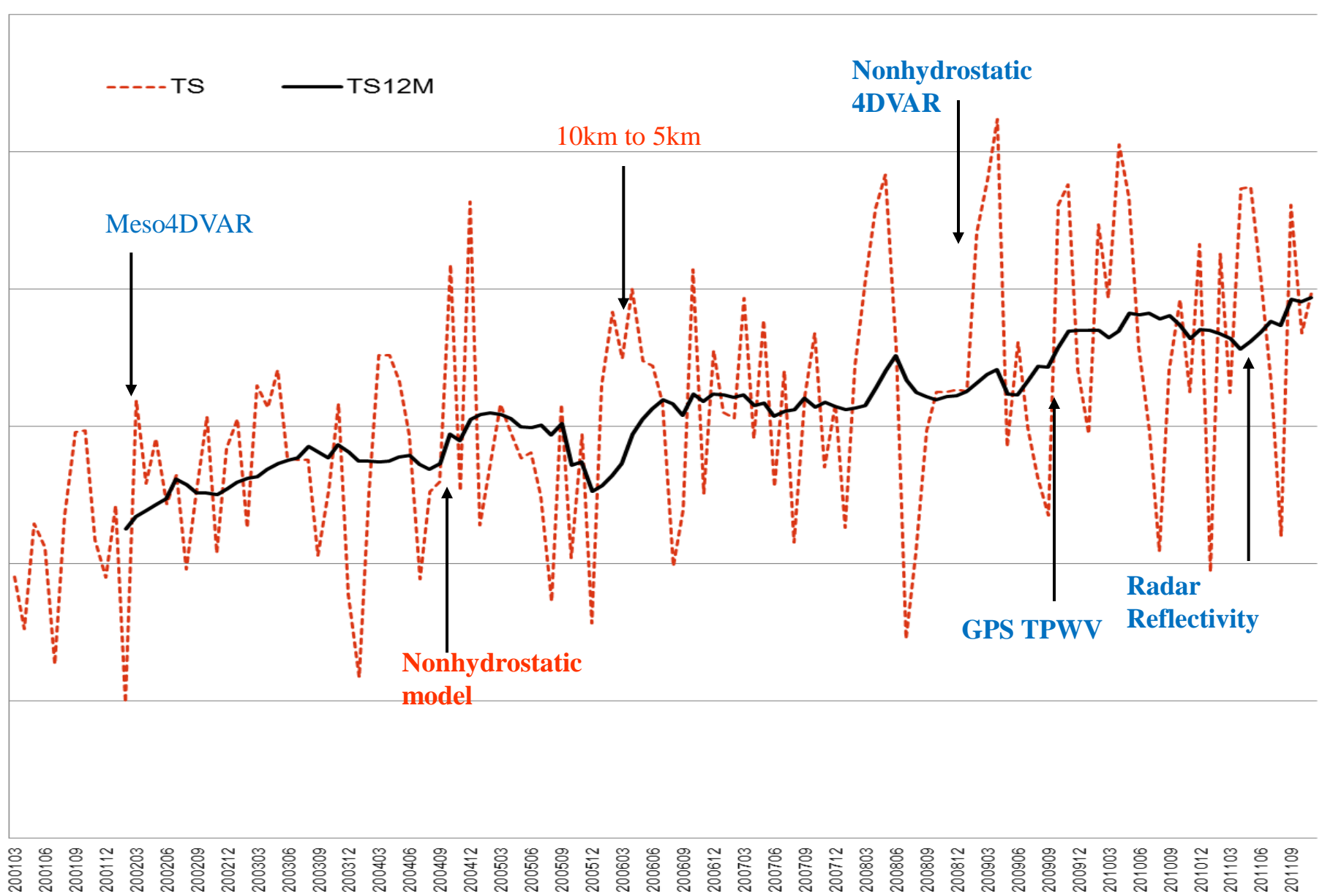


FT=24 from 2006 Aug 17 15UTC

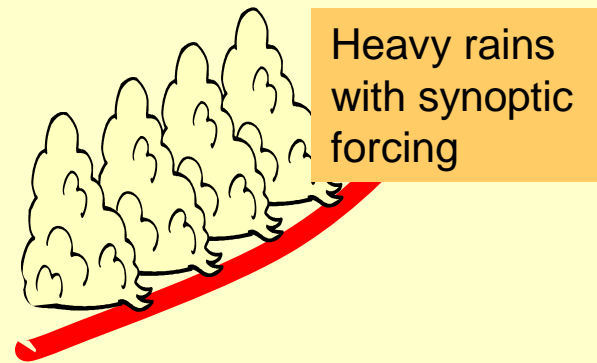
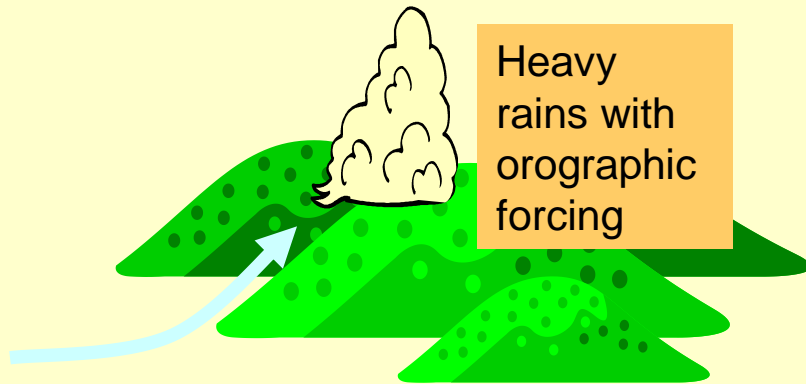
Sawada and Honda (2009)

# Threat score of MSM Mar.2001-Nov.2011 (FT=0-15)

MSM Threat Score 5mm/3h 20km verif. grid



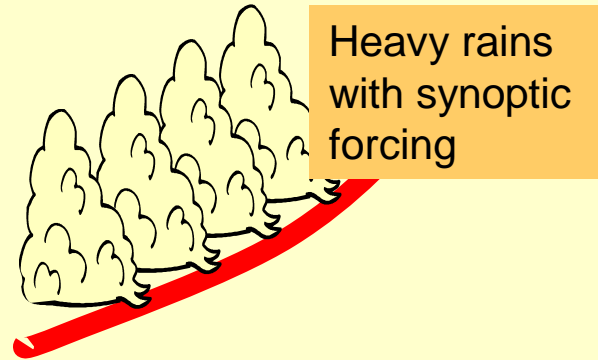
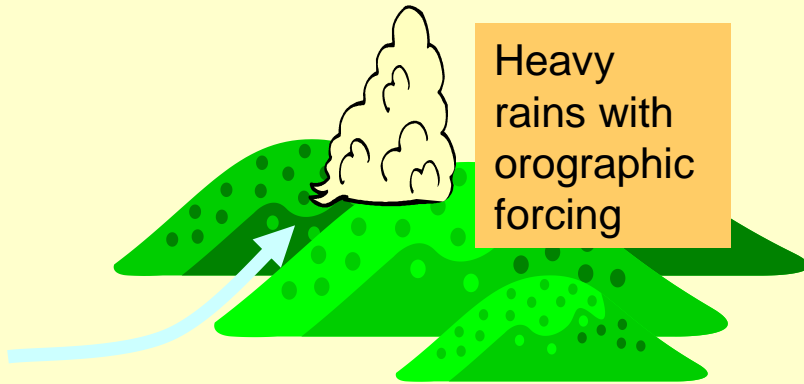
# Predictability of heavy rainfalls



- · relatively predictable in the current mesoscale NWP up to a point



# Predictability of heavy rainfalls

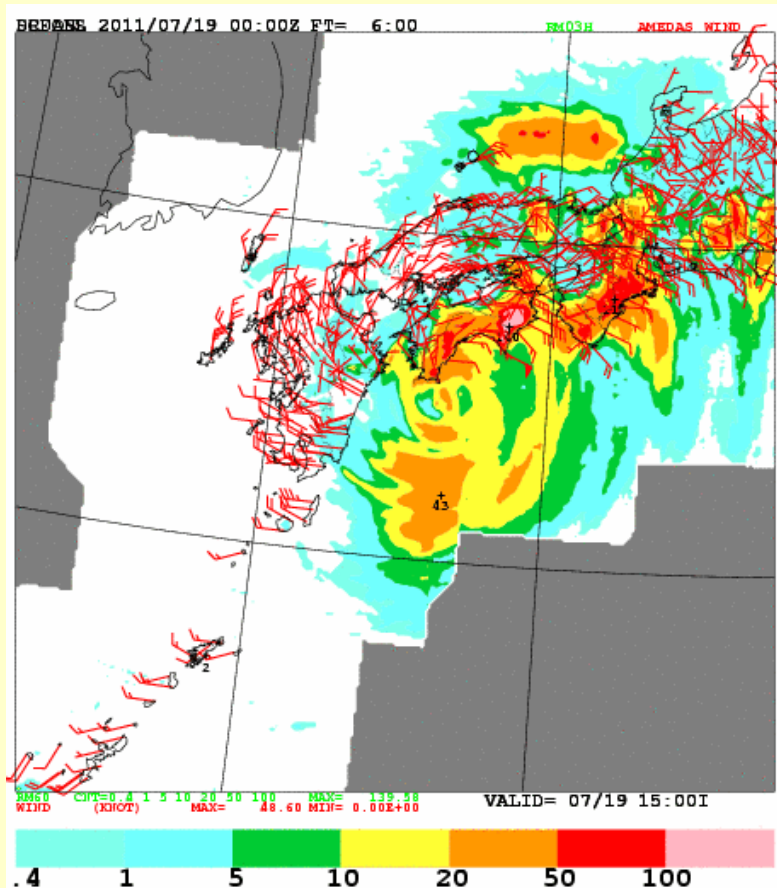


- • relatively predictable in the current mesoscale NWP up to a point

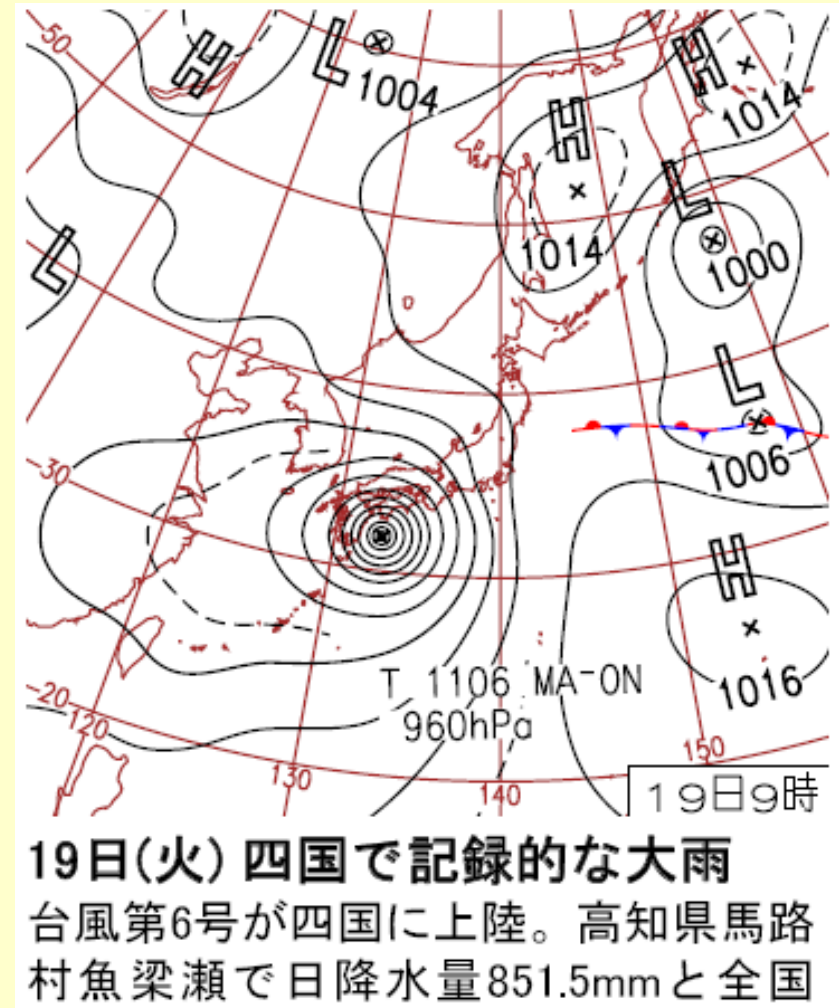


Position is fixed by forcing regardless the trivial errors in initial condition

# Example of orographic heavy rainfall



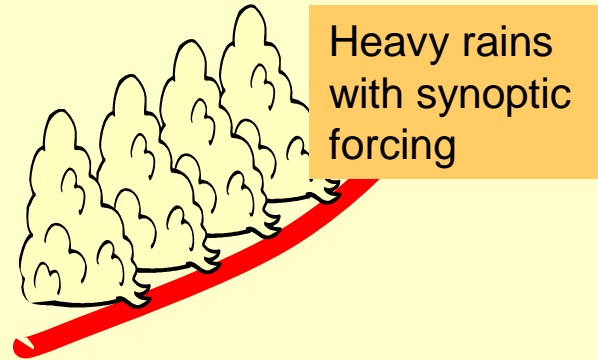
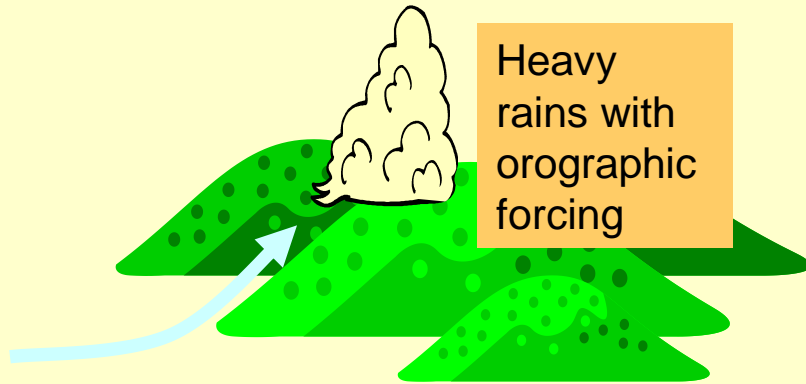
Radar-AMeDAS Observed rainfall  
03-06 UTC, 19 July 2011



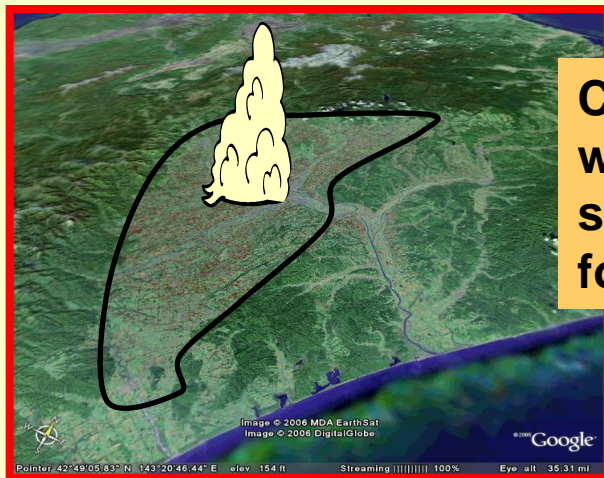
A strong typhoon (T201106 Ma-on) hit western Japan and a record breaking 851mm rainfall was observed in one day (19 July 2001).

MSM accurately predicted the orographically forced heavy rainfall.

# Predictability of heavy rainfalls



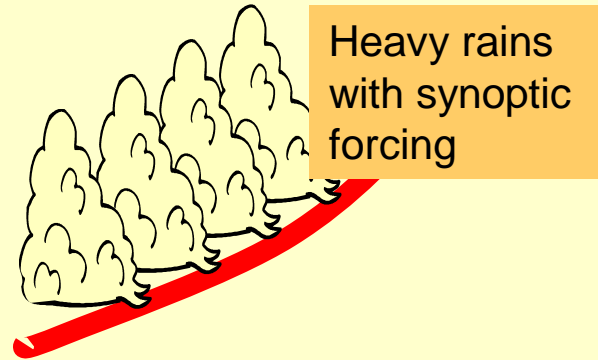
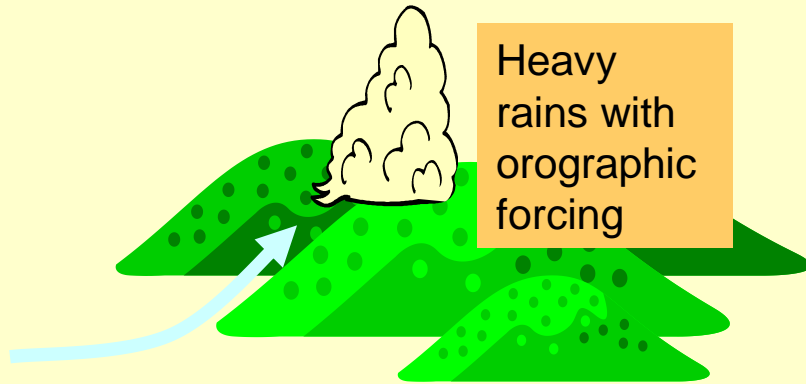
- · relatively predictable in the current mesoscale NWP up to a point



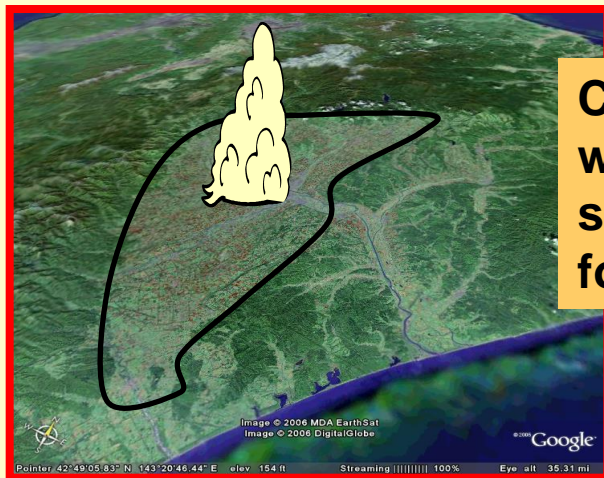
**Convective rains  
without strong  
synoptic/orographic  
forcing**

- · difficult to predict due to

# Predictability of heavy rainfalls



- · relatively predictable in the current mesoscale NWP up to a point



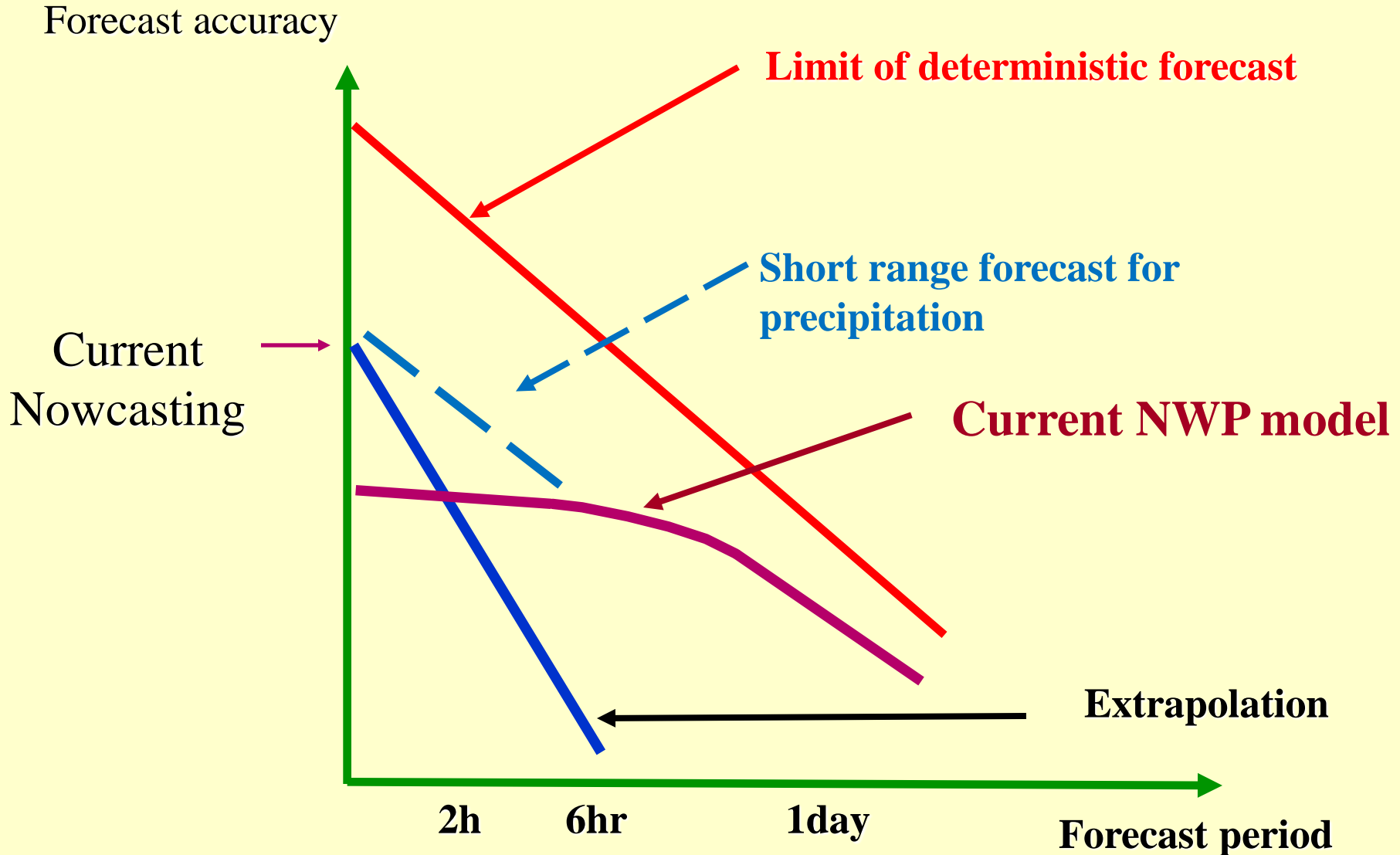
**Convective rains  
without strong  
synoptic/orographic  
forcing**

- · difficult to predict due to
- small horizontal/temporal scales
- phenomena in unstable atmosphere

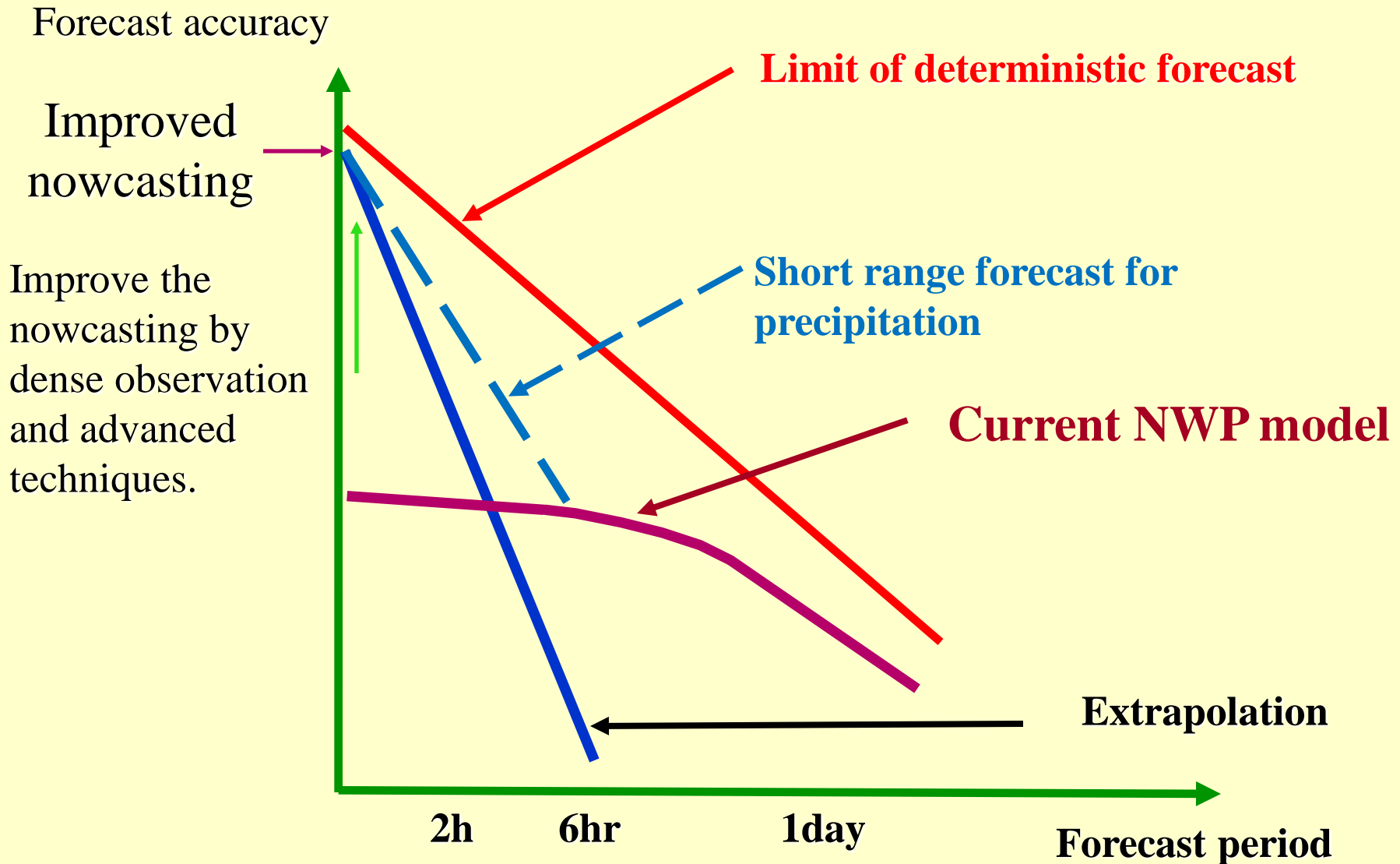


Result is very sensitive to small perturbations in initial conditions

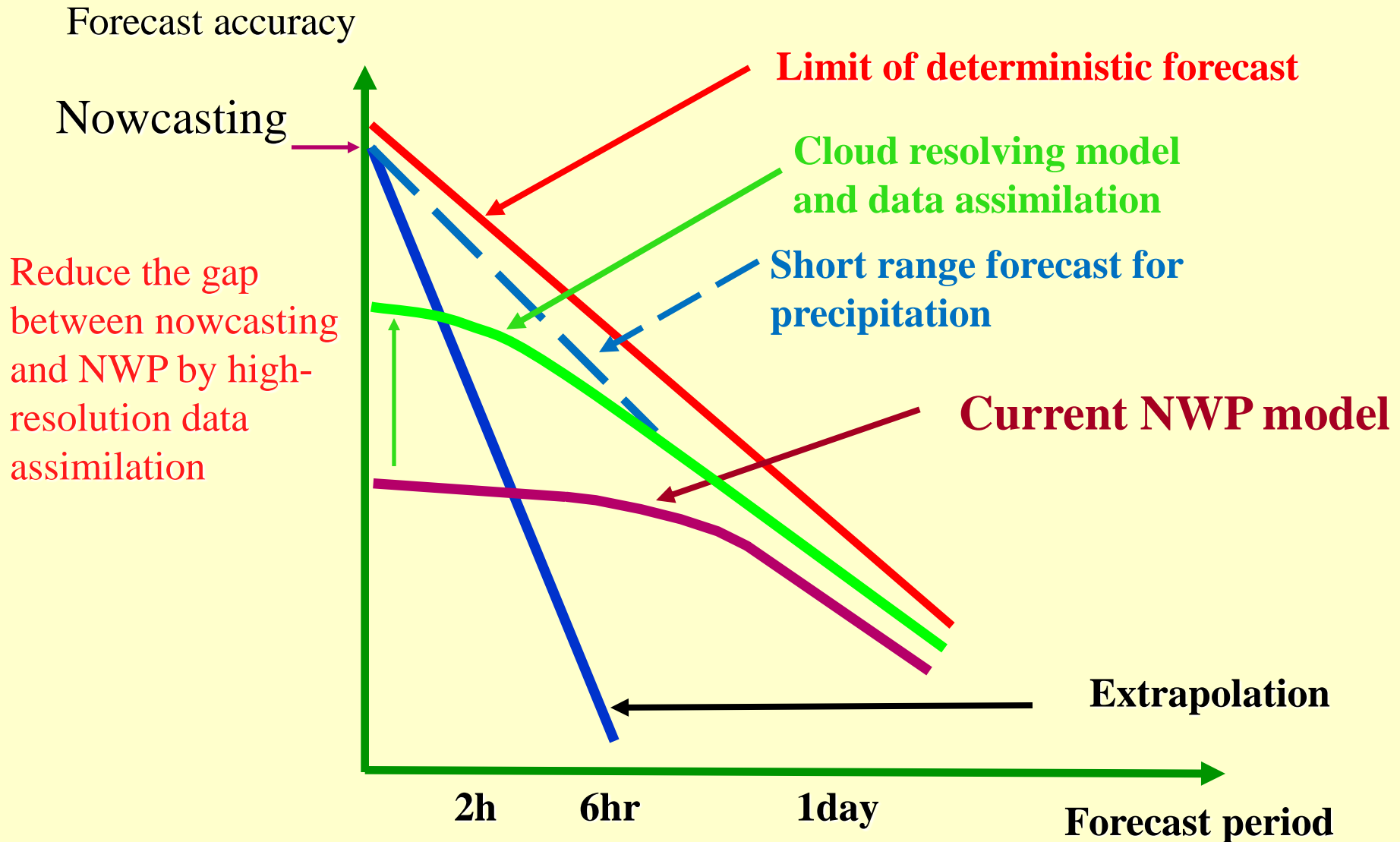
# Approaches to predict local heavy rain



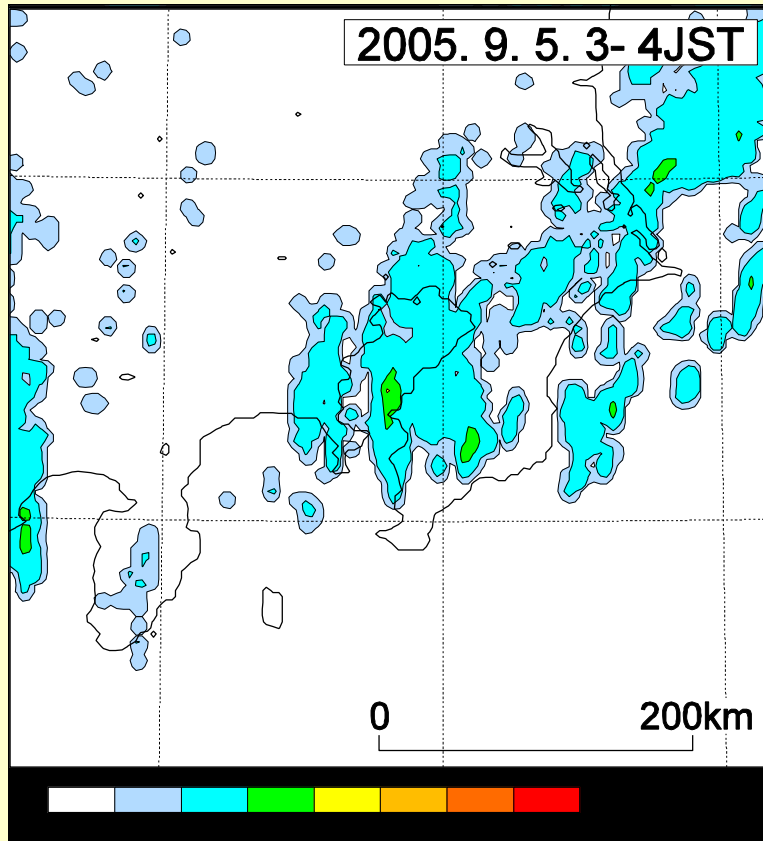
# Approaches to predict local heavy rain (1)



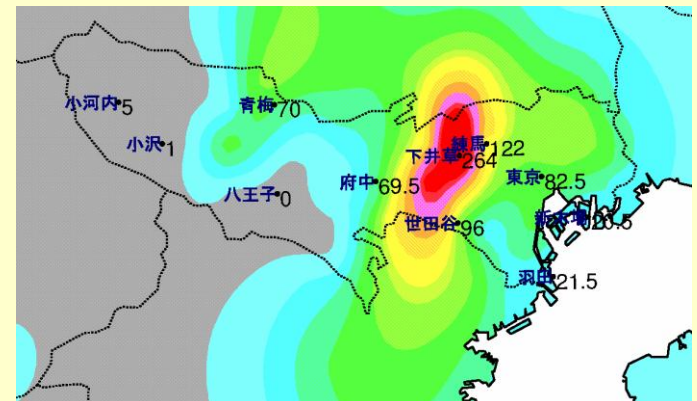
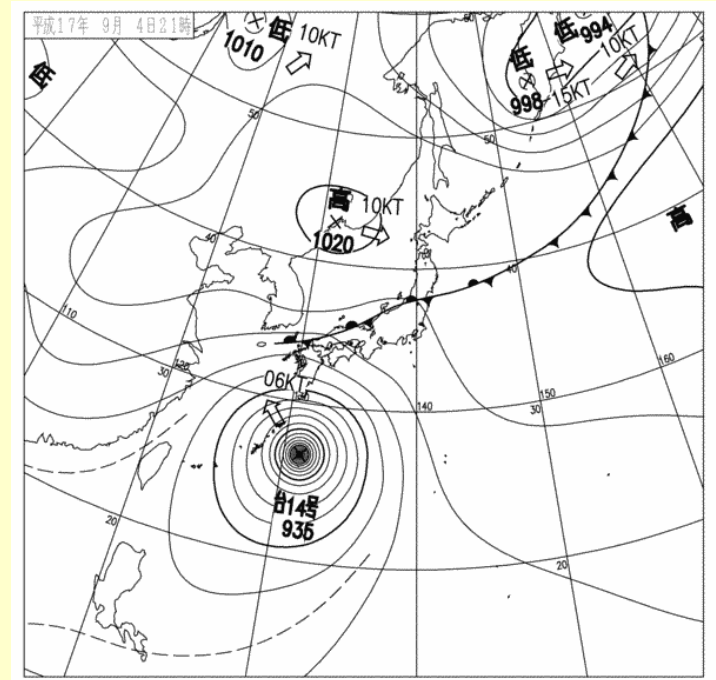
# Approaches to predict local heavy rain (2)



# Local Heavy rainfall on September 2005 in Tokyo



Local heavy rainfall on 4 September 2005  
100mm precipitation in 1 hour was observed in  
Tokyo. No significant disturbances over  
Tokyo metropolitan area.





# Cloud resolving 4DVAR with cloud microphysics

(Kawabata et al., 2011; *Mon. Wea. Rev.*)

Kessler warm rain process was implemented in LT/ADJ models.

4DVAR assimilation of

- Doppler Radar's Radial Winds
- **Radar Reflectivity**
- GPS precipitable water vapor
- Surface observations (wind, temperature)

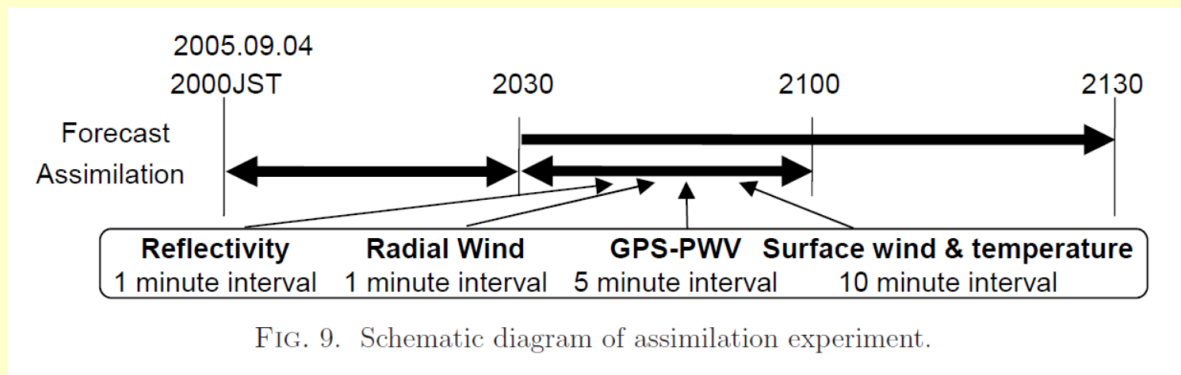
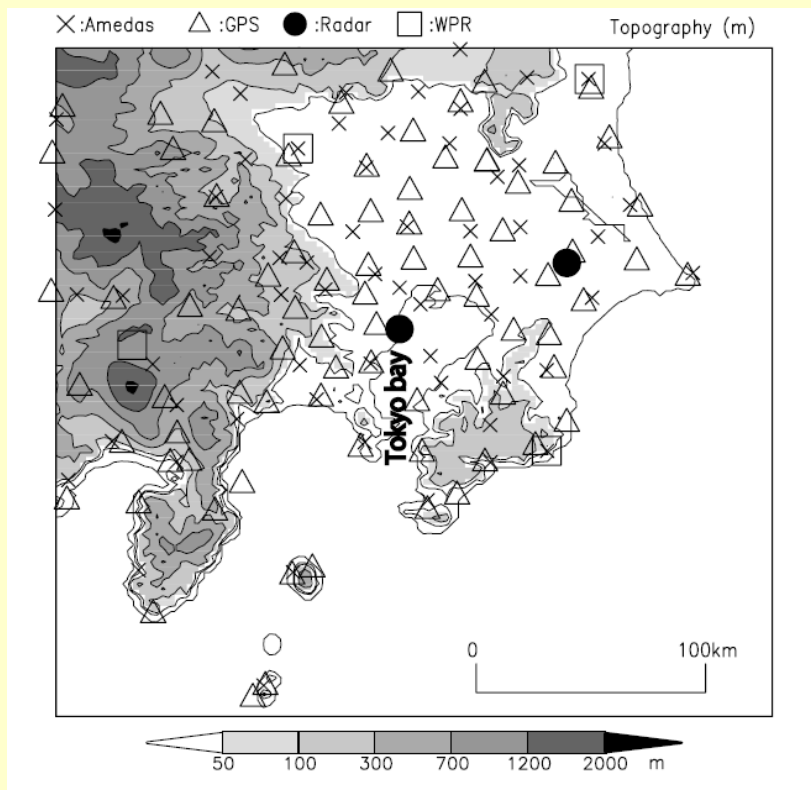
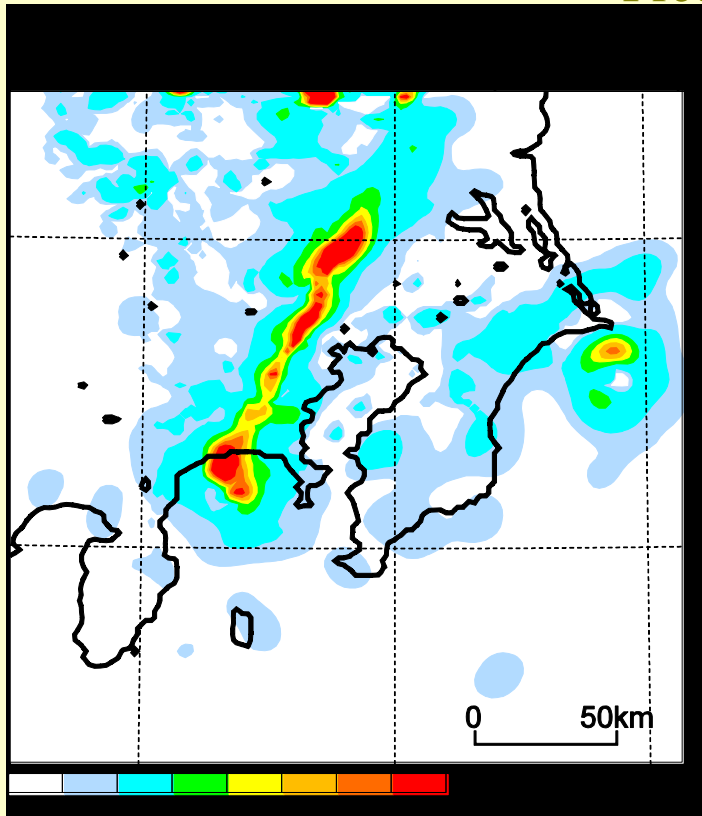


FIG. 9. Schematic diagram of assimilation experiment.

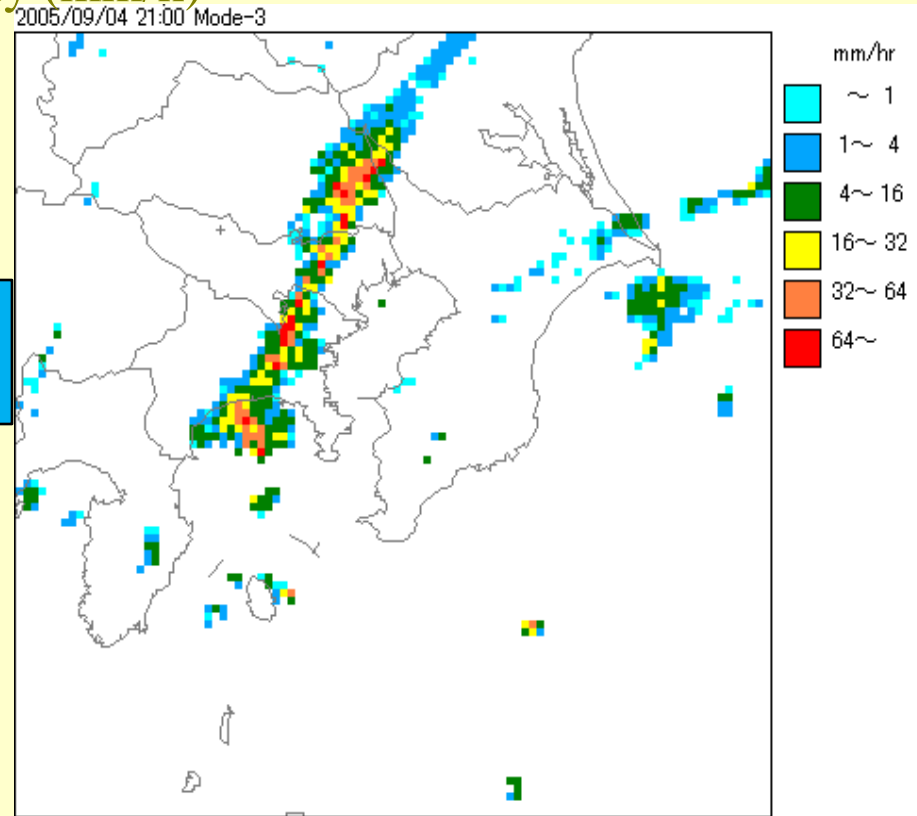
4DVAR analysis



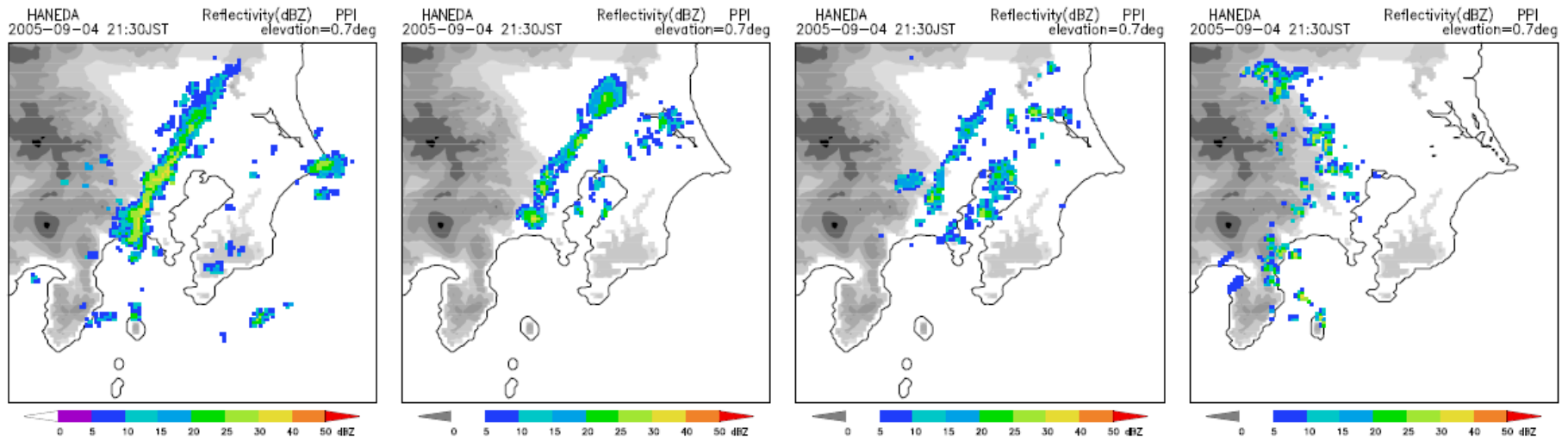
Assimilation of radar  
reflectivity 2030-2100JST

Precip. intensity (mm/h)

Observation



(Kawabata et al., 2011; *Mon. Wea. Rev.*)



2130 JST  
Obs

4DVAR with  
assimilation of  
radar reflectivity

4DVAR without  
radar reflectivity

1<sup>st</sup> guess

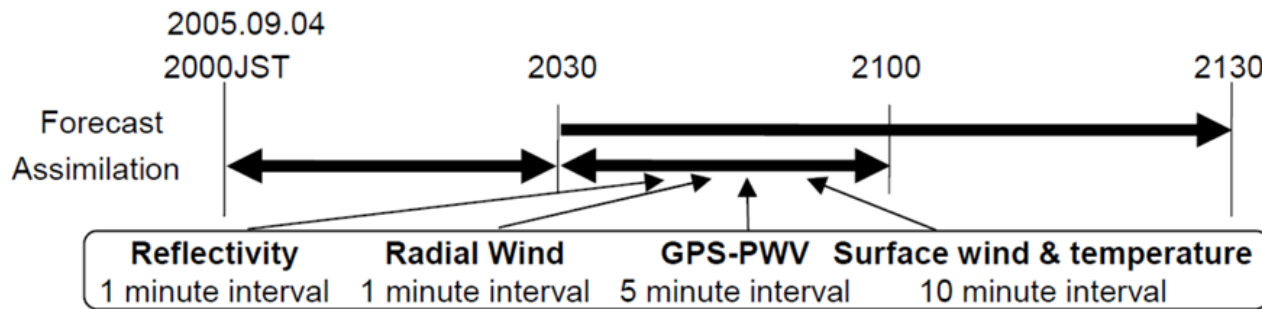


FIG. 9. Schematic diagram of assimilation experiment.

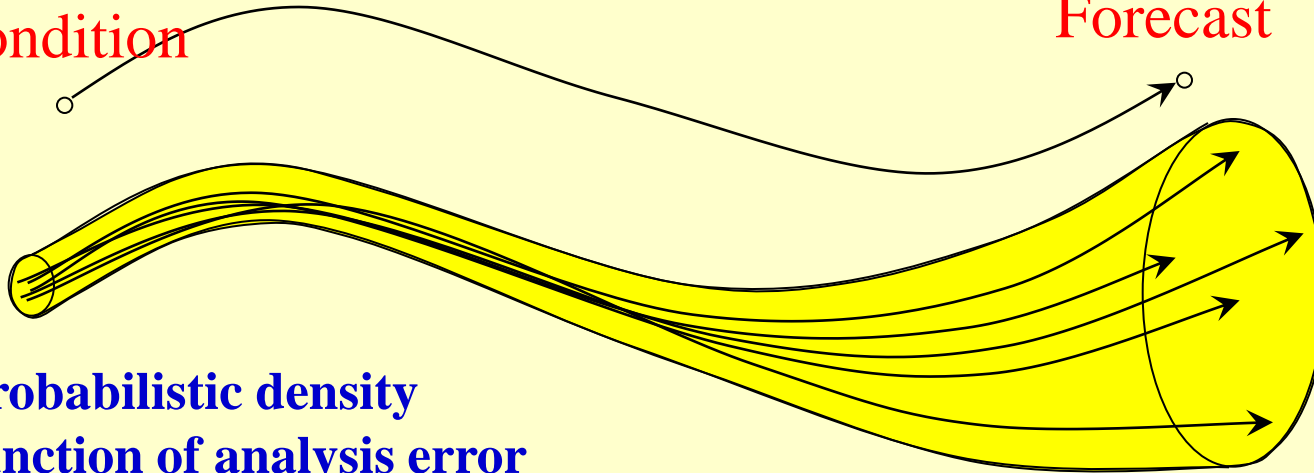
Kawabata, T., T. Kuroda, H. Seko, and K. Saito, 2011: A cloud-resolving 4D-Var assimilation experiment for a local heavy rainfall event in the Tokyo metropolitan area, *Mon. Wea. Rev.* **139**, 1911-1931.

# 4. Ensemble prediction

Initial  
condition

Forecast

deterministic  
prediction

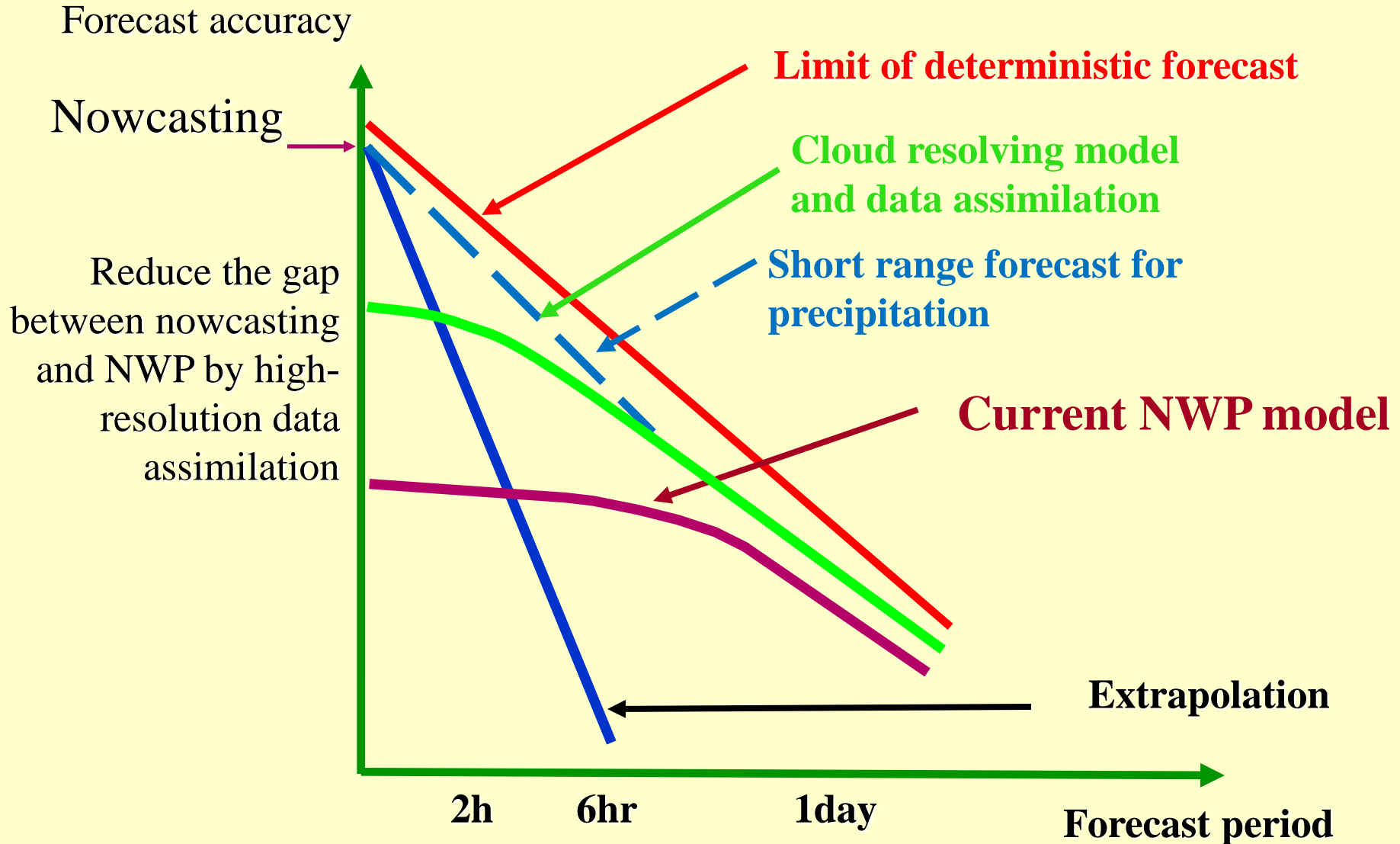


**Probabilistic density  
function of analysis error**

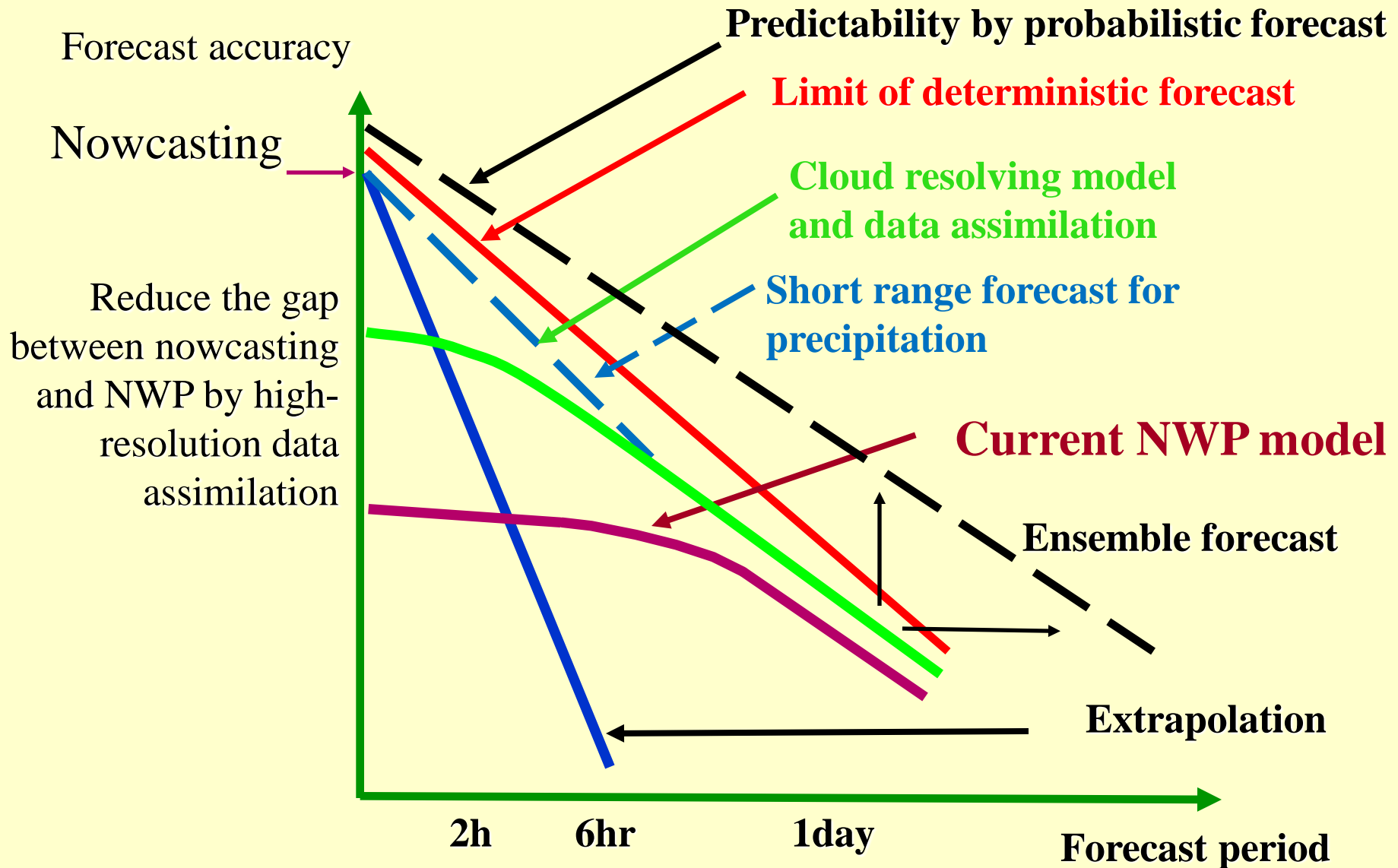
probabilistic  
prediction

Time integration of the probabilistic density function is practically impossible. In the ensemble forecast, finite members approximate the features of probabilistic density function of atmospheric states.

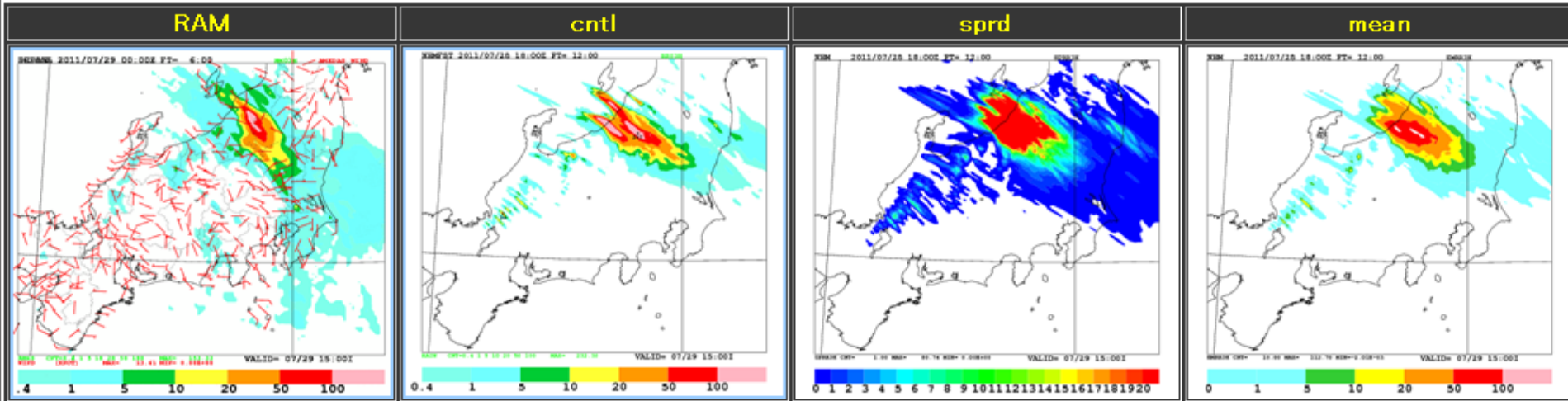
# Approaches to predict local heavy rain



# Approaches to predict local heavy rain (3)



# 2km ensemble prediction from JMA nonhydrostatic 4D-VAR analysis for 2011 Niigata-Fukushima heavy rainfall



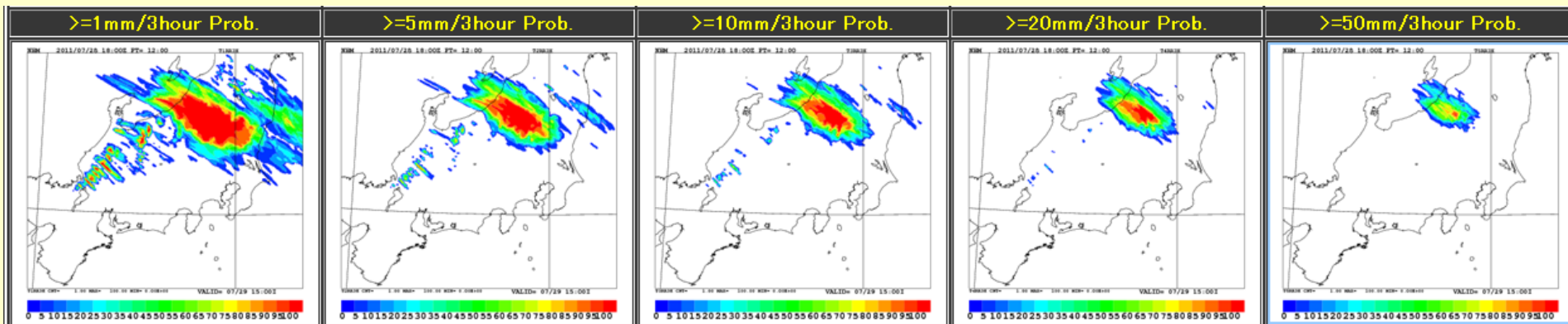
Observation

Control run

Ensemble spread

Ensemble mean

03-06 UTC, 29 July 2011



1mm/3h

5mm/3h

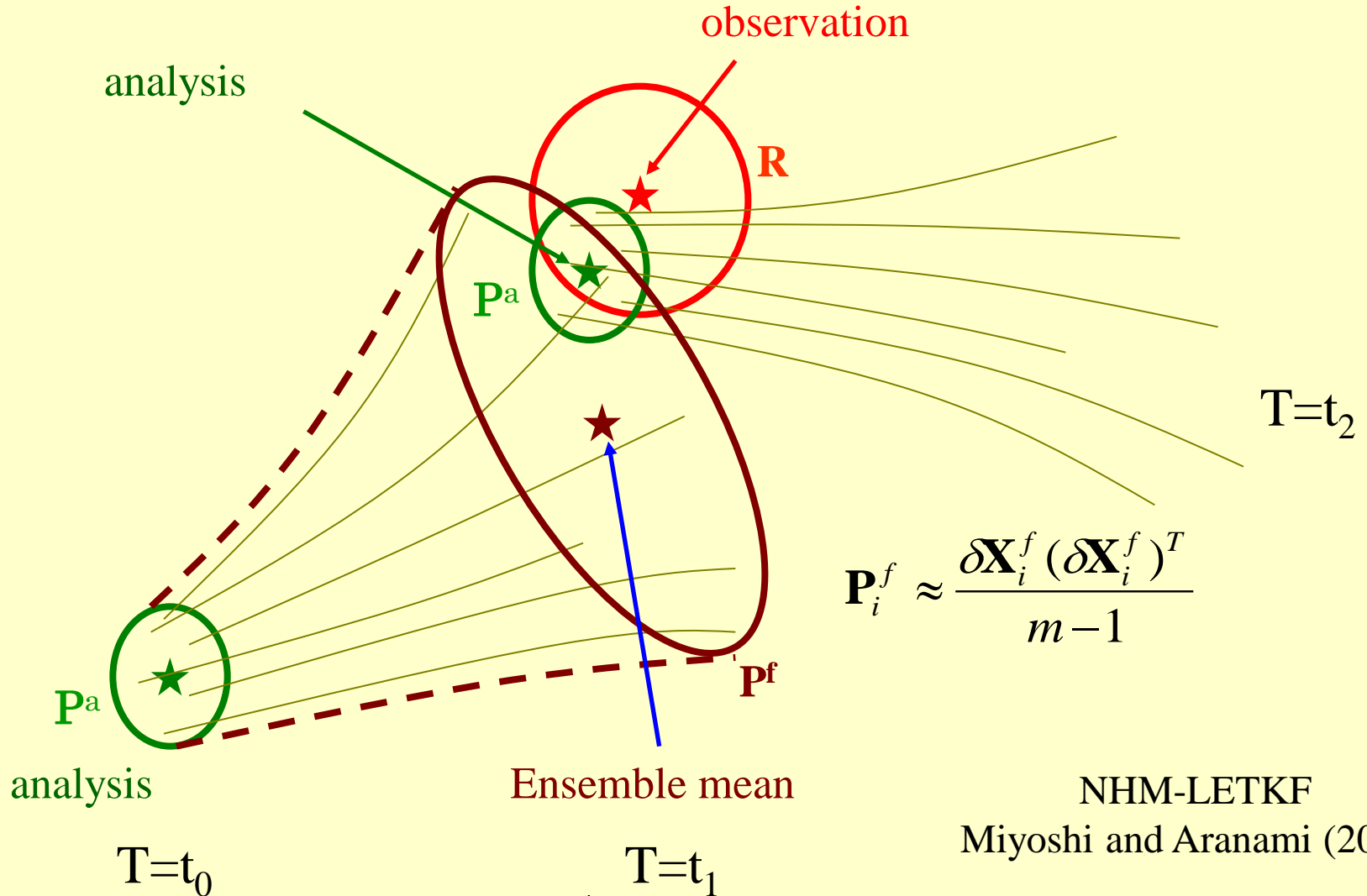
10mm/3h

20mm/3h

50mm/3h

Probability of precipitation at FT=18  
Solid probability even for 50mm/3h

# Ensemble Kalman Filter

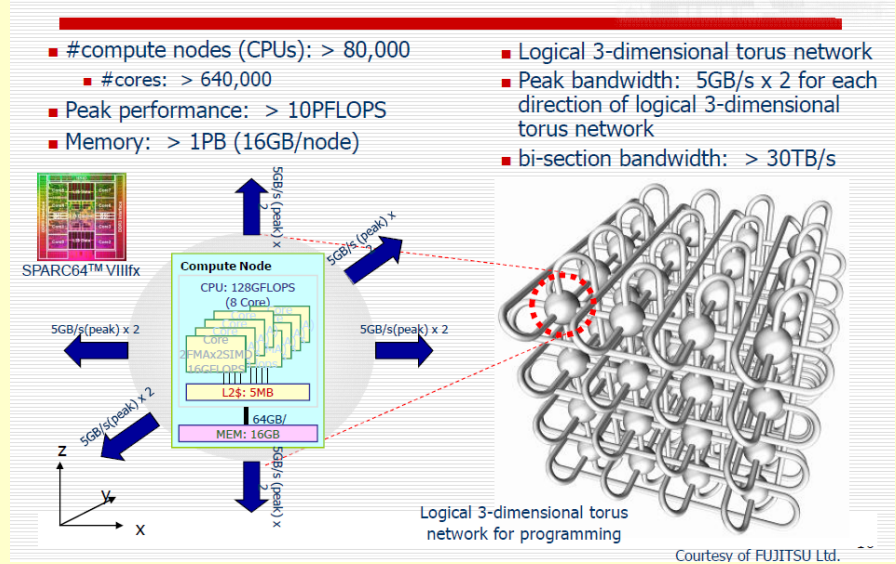


$$P_i^f \approx \frac{\delta X_i^f (\delta X_i^f)^T}{m-1}$$

$$\begin{aligned} \mathbf{X}^a &= \bar{x}^f e + \delta \mathbf{X}^f \left( \tilde{P}^a (\mathbf{H} \delta \mathbf{X})^T \mathbf{R}^{-1} (y^o - \overline{H(x^f)}) e + \sqrt{m-1} \mathbf{U} \mathbf{D}^{-1/2} \mathbf{U}^T \right) \\ &= \bar{x}^f e + \delta \mathbf{X}^f \tilde{P}^a (\mathbf{H} \delta \mathbf{X})^T \mathbf{R}^{-1} (y^o - \overline{H(x^f)}) e + \delta \mathbf{X}^f \mathbf{T} \end{aligned}$$



# 4. The K-Computer project



“HPCI Strategic Programs for Innovative Research (SPIRE)” is being carried out by RIKEN, with partners in industry, universities, national institutes under an initiative by MEXT

# The HPCI Strategic Programs for Innovative Research (2011.4-2016.3)

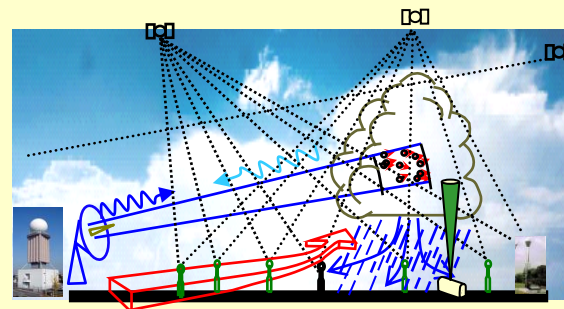
## Field 3: Weather, Climate and Environment Prediction for disaster prevention

### Sub theme ②: Super high performance mesoscale NWP

#### a. Cloud resolving 4DDA

- feasibility of dynamical prediction of local heavy rainfall in very sort range forecast

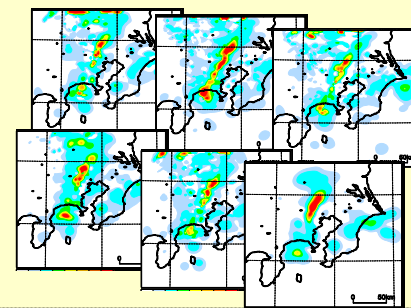
MRI, JMA, DPRI/Kyoto Univ., NIED, ISM



#### b. Cloud Resolving ensemble NWP and its verification

- quantitative prediction of the probability of local heavy fall with a lead time to disaster prevention

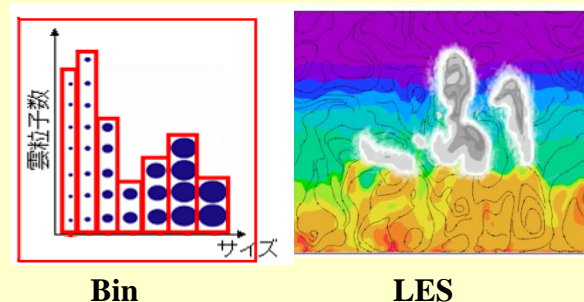
MRI, JMA, Tohoku Univ., DPRI/Kyoto Univ.



#### c. High performance atmospheric model

- Evaluation of model's uncertainty through super high resolution numerical experiments

JAMSTEC, MRI, Tokyo Univ., Nagoya Univ., etc.



## Application example: Torrential rain in Kobe City on July 28, 2008



(a) 14:30 (-0.37m)



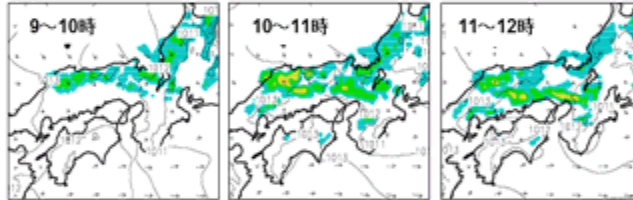
(b) 14:40 (-0.33m)



(c) 14:50 (1.01m)

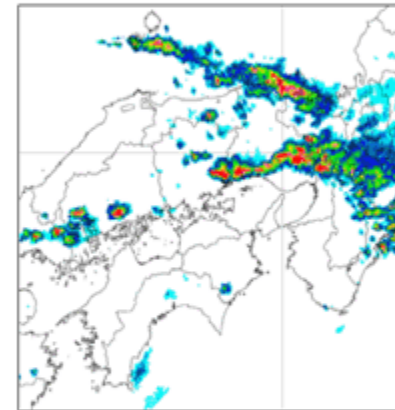
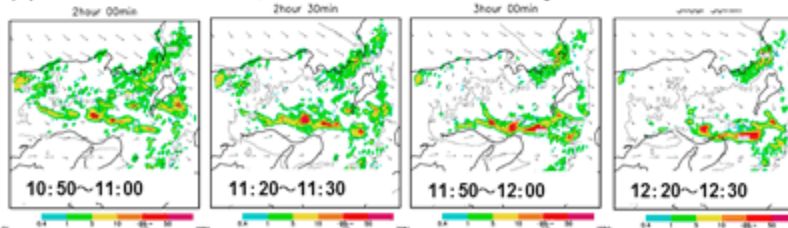
The swollen Togagawa River in kobe city  
(killed 5 people)

(a) Grid interval = 5 km; initial value = 9 a.m. on July 28



Higher-resolution

(b) Grid interval = 1.6 km; initial value = 9 a.m. on July 28

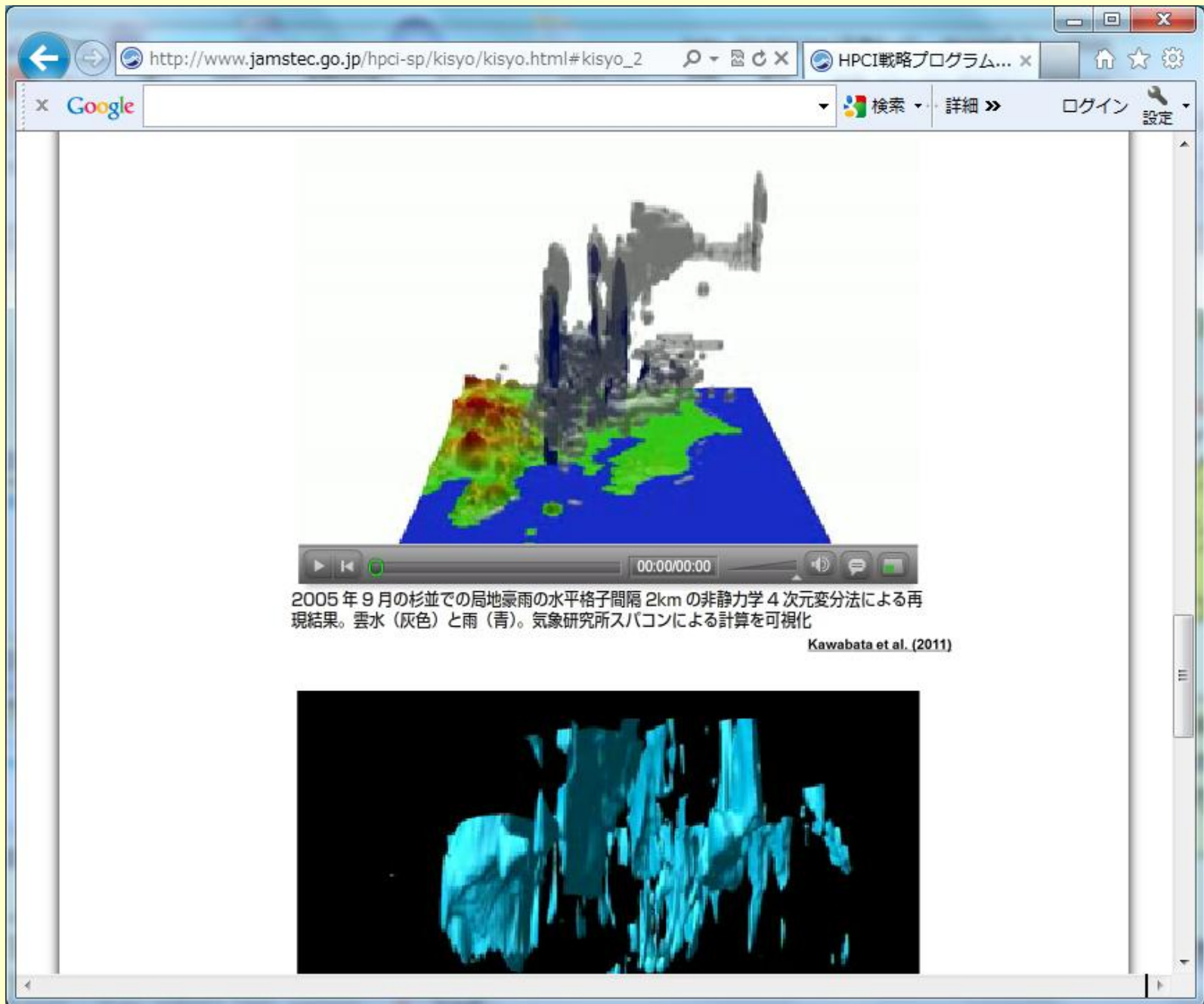


Precipitation from 1 p.m. to 2 p.m. on July 28  
observed by JMA's radars

Data assimilation experiment of GPS total  
precipitable water vapor using the local  
ensemble transform Kalman filter

Cloud resolving downscaling with a horizontal  
resolution of 1.6 km

Seko et al. (2011)



2005年9月の杉並での局地豪雨の水平格子間隔2kmの非静力学4次元変分法による再現結果。雲水（灰色）と雨（青）。気象研究所スパコンによる計算を可視化

Kawabata et al. (2011)

## The 3rd Research Meeting of Ultrahigh Precision Meso-Scale Weather Prediction

### Date/Time

March 21, 2013 (Thu) 09:00~17:30

### Venue

Large Conference Room, Nichii Gakkan Kobe Port Island Center  
 TEL : +81-78-304-5991  
 7-1-5, Minatojima-Minamimachi, Chuo-ku, Kobe 650-0047, Japan

### Program

March 21		
09:00-09:20	Opening Address	Akihide Segami (MRI)
	Introduction	Tatsushi Tokioka (JAMSTEC) Kazuo Saito (MRI/JAMSTEC)
09:20-10:40	Development of cloud-resolving data assimilation systems	Chair: Tadashi Tsuyuki (MRI)
	Keynote Speech	Ming Xue (University of Oklahoma)
11:10-12:30	Development of a regional cloud-resolving ensemble analysis and forecasting system	Chair: Hiromu Seko (MRI/JAMSTEC)
14:00-17:00	Address	Tetsuyuki Muramatsu (MEXT)
	Development and basic research for the ultrahigh precision regional models	Chair: Fujio Kimura (JAMSTEC)
	Keynote Speech	Song-You Hong (Yonsei University)
17:00-17:30	General Discussion	

### Registration: No fee required

Those who are interested in participating are required to send an email to the following address by March 3. Participants in the lunch and dinner also need to be registered in advance.

## HPCI Strategic Programs for Innovation Research, Field 3 Prediction of Planet Earth Variations for Mitigating Natural Disasters Research and Development Project (2)



## The 3rd Research Meeting of Ultrahigh Precision Meso-Scale Weather Prediction

March 21, 2013 (Thu)

**Venue:** Large Conference Room, Nichii Gakkan Kobe Port Island Center

**Registration fee:** No fee

JAMSTEC, MRI/JMA

# Summary

- Prediction of weather is performed by numerical computation.
- Performance of state of the art mesoscale NWP has been remarkably improved, but still storm scale prediction is challenging.
- High resolution data assimilation and ensemble prediction are necessary. The K-computer will reduce compromise of resolutions and ensemble members and show a prototype of the future NWP system.

# Thank you

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